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Visual and tactile sensory systems share common features in object recognition

Abbreviated Title: Shared visual and tactile perceptual spaces

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1 **Abstract**

2 Although we use our visual and tactile sensory systems interchangeably for object recognition on a
3 daily basis, little is known about the mechanism underlying this ability. This study examined how 3D
4 shape features of objects form two congruent and interchangeable visual and tactile perceptual spaces
5 in healthy male and female participants. Since active exploration plays an important role in shape
6 processing, a virtual reality environment was used to visually explore 3D objects called digital
7 embryos without using the tactile sense. In addition, during the tactile procedure, blindfolded
8 participants actively palpated a 3D-printed version of the same objects with both hands. We first
9 demonstrated that the visual and tactile perceptual spaces were highly similar. We then extracted a
10 series of 3D shape features to investigate how visual and tactile exploration can lead to the correct
11 identification of the relationships between objects. The results indicate that both modalities share the
12 same shape features to form highly similar veridical spaces. This finding suggests that visual and
13 tactile systems might apply similar cognitive processes to sensory inputs that enable humans to rely
14 merely on one modality in the absence of another to recognize surrounding objects.

15 **Significance Statement**

16 Human brains are able to precisely and rapidly identify tactile and visual objects, an ability indicating
17 that we use visual and tactile information interchangeably to recognize surrounding objects. This study
18 examined the role of shape features that enable human reliance on visual or tactile sensory modalities
19 for object recognition and provides evidence that the visual and tactile modalities not only generate
20 two highly congruent perceptual spaces but also use the same shape features to recognize a novel
21 object. This finding contributes to explaining why visual and tactile senses are interchangeable.

22 **Introduction**

23 Our ability to correctly and quickly recognize an object in both the tactile and visual modalities raises
24 the question of how humans form representations of their surroundings using the visual or tactile
25 system, as well as which common object features play a role in object perceptions to mediate that
26 interchangeability?

27 Shape is a crucial feature for efficiently interacting with objects in both the visual and tactile domains
28 (Rosch, 1988). While much is known about visual shape processing (Haushofer et al., 2008; Peelen et
29 al., 2014), less information is available regarding tactile shape processing (Hernández-Pérez et al.,
30 2017; Klatzky et al., 1985; Metzger et al., 2019). A series of studies comparing visual and tactile
31 perceptual spaces with familiar objects have revealed that the human perception of familiar objects is
32 not solely determined by the physical features of objects but is influenced by high-level cognitive
33 abilities, including memory (Amedi et al., 2002; Haag, 2011; Metzger and Drewing, 2019; Norman et

34 al., 2008) and prior knowledge of objects for integrating sensory systems (Ernst and Bühlhoff, 2004).
35 While other studies have used parametric shape models, such as shell-shaped 3D objects (Gaißert et
36 al., 2011, 2010a, 2008; Gaissert and Wallraven, 2012), it is difficult to capture the shape complexity of
37 natural objects with parametric approaches and avoid possible confounds or special cases in object
38 shapes (Haushofer et al., 2008; Lee Masson et al., 2016). To bridge the gap between highly familiar
39 and novel 3D objects, we used a virtual phylogenesis (VP) algorithm to simulate the biological process
40 and create a unique set of novel naturalistic 3D objects: the so-called digital embryos (Hauffen et al.,
41 2012).

42 Although active object exploration leads to faster recognition (Harman et al., 1999), facilitates visual
43 object learning (Tsutsui et al., 2019), and benefits the mental rotation of three-dimensional objects
44 (James et al., 2002), visual active exploration integrates tactile cues regarding object size and texture
45 in addition to visual information (Savini et al., 2010). To avoid such interaction, recent studies have
46 displayed 3D objects on 2D screens or have required the experimenter to rotate the objects (Lee and
47 Wallraven, 2013). To investigate the visual and touch senses separately and maintain this separation,
48 the study by Gaißert et al. (2010b) utilized a head-mounted display (HMD) to present virtual 3D
49 objects. Their HMD was set up in a darkened room which is isolated and greatly dissimilar to real-life
50 conditions. In our current study, a virtual room was chosen to simulate a natural situation that
51 resembles real-life conditions. We used virtual reality (VR) technology too to minimize tactile
52 influences during active exploration and thus eliminate the influence of the experimenter and tactile
53 information in visual exploration (James et al., 2002; Van Veen et al., 1998).

54 Recent studies addressing the link between perceptual spaces from different sensory systems used
55 similarity judgments (Cooke et al., 2007; Gaißert et al., 2011; Lee and Wallraven, 2013; Op De Beeck
56 et al., 2008), as well as multidimensional scaling (MDS) (Cooke et al., 2005a; Gaissert and Wallraven,
57 2012; Jaworska and Chupetlovska-Anastasova, 2009; Lee Masson et al., 2016; Steyvers, 2002). These
58 studies demonstrated that visual and tactile perceptual spaces were highly congruent and that physical
59 spaces derived from adjusting parameters in a parametric model can be reconstructed in vision, as well
60 as in touch. Still, which complex shape features are used by both visual and tactile modalities to
61 represent objects in the brain in similar perceptual spaces remains unknown. Further, this study
62 assessed how a combination of shape features affects the perceived similarity between objects
63 compared to a single shape feature.

64 We investigated the role of shape in reconstructing the same perception of objects in visual and tactile
65 systems to mediate interchangeability between both modalities. To this end, we extracted
66 computational features from the digital embryos created by our VP algorithm to assess the similarity
67 between visual and tactile perceptual spaces. Our results show that the visual and tactile modalities not
68 only generate two highly congruent perceptual spaces but also share the same shape features to

69 recognize the novel object. This finding contributes to explaining why visual and tactile senses can be
70 interchangeable.

71 **Material and methods**

72 **Participants**

73 A total of 50 volunteers (25 female, mean age = 24.3 ± 3.7 years, all right-handed) participated in the
74 behavioral experiments. Twenty-five of them (13 female, mean age = 23.7 ± 2.6 years) participated in
75 the visual similarity judgment experiment, and the remaining 25 (13 female, mean age = 24.9 ± 4.6
76 years) participated in the tactile similarity judgment experiment. All participants reported normal or
77 corrected-to-normal vision, normal color vision, no history of severe hand injuries, and no history of
78 neurological disorders. All participants were naïve to the purpose of the experiment and provided
79 informed written consent before starting the experiment. The participants received 10 € per hour for
80 their participation. The local ethics committee of the Medical Faculty of Ruhr-University Bochum
81 (No. 17-6184) approved all experiments.

82 **Generation of three-dimensional objects**

83 To implement natural object properties and prevent evoking memories of familiar objects that might
84 influence perceptual processing, we created naturalistic 3D objects (referred to as digital embryos)
85 using a virtual phylogenesis (VP) algorithm (Brady and Kersten, 2003; Hauffen et al., 2012). Digital
86 embryos were created from a uniform icosahedron as an ancestor that was subsequently changed by
87 simulating the biological process of embryogenesis: cell division, cell growth, and cell movement (for
88 more details, see <http://hegde.us/digital-embryos/>). In the present study, 16 embryos from two
89 categories (eight objects per category) of the third generation were selected (Figure 1A). This
90 algorithm benefits from the independent creation of shape variations within and across generated
91 categories that are not imposed by an experimenter. In addition, the features of digital embryos are
92 very similar to those of natural objects. Since the purpose of the current study was to identify shape
93 features that were informative for similarity ratings between objects in both modalities, features such
94 as weight, color, size, and material were kept constant for all objects. It is important to note that the
95 overall appearance of objects within each category was similar (based on a pilot experiment) and
96 distinguishing embryos between both categories was not trivial.

97 In the visual experiment, we presented the stimuli in a 3D virtual reality environment to allow the
98 participants to perform a natural exploration of objects from every possible angle without actually
99 touching them. For this purpose, the generated digital embryos were imported into the Unity game
100 engine 2017.2.0b8 (Unity Technologies, USA) that delivered the 3D virtual environment wherein the
101 similarity judgment experiment was performed. All virtual stimuli were given white matte materials.

102 For the tactile experiment, tangible hard plastic models of objects were printed using a 3D printer
103 (Replicator 2X, MakerBot Industries, LLC One MetroTech Center, 21st Fl, Brooklyn, NY 11201
104 USA). The printed objects were sanded with sandpaper to remove any blemish and produce similarly
105 smooth textures and deliver a similar tactile experience. The dimensions of the printed embryos were
106 matched with those presented in the virtual environment.

107 **Experimental procedures**

108 A standard similarity rating task based on a Likert-type scale was designed for both visual and tactile
109 modalities. Participants were presented with object pairs and asked to rate the similarity between the
110 two presented objects on a seven-point scale from completely dissimilar (1) to identical (7). As there
111 was no definition for similarity in either experiment, the participants were required to select the
112 feature(s) on which they based their ratings. Furthermore, the participants were not informed that there
113 were two different object categories. A total of 136 pairs of objects $[(16 \times (15/2) + 16)]$ were
114 presented in random order. A pilot study (eight participants [n=4, visual experiment]) was conducted
115 to determine the required object exploration time in the visual and tactile domains, as well as the
116 necessary number of repetitions for each pair. Based on these results and previous studies that
117 demonstrated that participants' responses remained constant over repeated stimulus presentations
118 (Gaissert and Wallraven, 2012), each pair was presented only once in the main experiment. In
119 addition, during our pilot experiment, subjects needed more time to gather relevant tactile than visual
120 information; previous studies of cross-modal perception similarly found that tactile exploration
121 requires twice as much time as visual exploration (Erdogan et al., 2015; Gaissert and Wallraven, 2012;
122 Norman et al., 2003). Therefore, we decided on 4 s for visual exploration and 8 s for tactile
123 exploration.

124 In both experiments, the response time required to provide a similarity rating was not restricted.
125 Participants were instructed to use the full range of the scale during the experiment and to focus on the
126 object features. After each pair, verbal responses were recorded by the experimenter. There were three
127 optional breaks during both the visual and tactile experiments. Generally, the visual and tactile
128 experiments had durations of approximately 1 and 1.5 h, respectively.

129 After performing the task, participants completed a survey querying the object features that were
130 important for guiding their respective similarity ratings. The listed features included (i) global shape,
131 (ii) pattern of branches, (iii) number of branches, (iv) size of branches, (v) global pattern, (vi)
132 concavity and convexity or curvature, (vii) texture, (vii) material, (ix) color, and (x) weight.

133 **Visual experiment**

134 The experiment was performed in a virtual office environment. The participants sat on a real chair in
135 front of a virtual desk in a virtual office. Two perspectives in the office are presented in Figure 1B.
136 The color of the walls, furniture, and lighting of the virtual room were chosen to render the details of
137 our stimuli to be easily discernible for the participants. This virtual environment was displayed on an
138 HTC Vive headset (www.vive.com, developed by HTC and Valve Corporation) with a resolution of
139 1080×1200 pixels per eye (2160×1200 pixels combined), 110° field of view, at a 90 Hz refresh rate.
140 By using a Vive wireless controller, participants could virtually grasp, pick up, and rotate an object
141 freely to investigate it under different angles. The stimuli were presented at random orientations in
142 front of the participants on a virtual desk.

143 Since the environment was completely new to the participants, they were familiarized with the VR
144 environment, the proper use of the controller, and the 3D digital embryos before performing the main
145 task. First, participants were asked to look around the virtual environment in order to become familiar
146 with the virtual office and thus avoid any distractions during the main experiment. Second,
147 participants were asked to visually examine all 16 3D digital embryos presented in random order for
148 up to 8 s each to become familiar with their shape variations. Before the main experiment, the
149 participants performed ten training trials that were excluded from the final analysis. In each trial of the
150 main experiment, object pairs were presented in a random orientation in front of the participants at a
151 fixed location on the virtual table (Figure 1C). The participants were given 4 s to explore the first
152 object. After a 1-s delay, the second object was presented for 4 s. Afterward, participants verbally
153 reported the perceived rate of similarity (between 1 and 7) of the pair with no time restriction. Rating
154 values were recorded by the researcher.

155 **Tactile experiment**

156 Blindfolded participants were comfortably seated on a table with a sound-absorbing surface. They
157 wore sleep masks during the entire experiment so that they had to explore the objects tactilely, without
158 vision. As in the visual experiment, participants were familiarized with the stimulus set before the start
159 of the main experiment and explored each stimulus for 12 s. The main task was started by performing
160 10 test trials that were not considered for the final analysis. Participants were allowed to freely explore
161 and palpate objects with both hands in a natural way with no restrictions.

162 Each trial started with an object placed in the hands of the participant. After a start signal (a beep tone,
163 5 kHz, 300 ms) was played via the speaker, the exploration time started. A stop signal (same beep tone
164 as at the start of exploration) played after 8 s indicated the end of exploration time, and the participant
165 was required to put the object back on the table. At this moment, the experimenter replaced the first
166 object with a second, and the exploration began following after the start signal. After 8 s, the

167 participant was required to put the second object back on the table immediately after hearing the stop
168 signal and rate the similarity between them verbally (see Figure 1D).

169 **Statistical Analysis**

170 **Analysis of the similarity ratings**

171 The ratings of all participants were averaged to obtain average similarity matrices for both the visual
172 and tactile modalities. The correlation between the average similarity matrices of both modalities was
173 calculated to analyze the degree of similarity between object explorations in the visual and tactile
174 domains. Similarity matrices were converted to dissimilarity matrices by subtracting the similarity
175 ratings from the maximum rating value of 7. To reconstruct the topology of the perceptual spaces, a
176 non-metric multidimensional scaling analysis (MDS) implanted in MATLAB (V.2019b, The Math
177 Works, USA) was applied to the visual and tactile group dissimilarity matrices (Cooke et al., 2007;
178 Gaissert and Wallraven, 2012; Lee Masson et al., 2016). The MDS algorithm represents each object as
179 a single point on a multidimensional scale. To determine the number of dimensions sufficient for
180 explaining the data, the stress value was calculated for each dimension value from 1 to 10 (Cox and
181 Cox, 2001; Steyvers, 2002). A statistical elbow in the stress plot indicates the number of dimensions
182 required to represent the data. As the elbow in the stress plot represents the adequate dimension, a
183 plateau in the squared correlation plot (RSQ values which are the proportion of variance of the
184 similarity data) illustrates sufficient dimension to visualize the data (Cooke et al., 2006, 2005a). An
185 ALSCAL MDS algorithm implanted in SPSS (IBM SPSS Statistics for Windows, Version 26.0.
186 Armonk, NY: IBM Corp) was used to calculate the RSQ values. The weight of the first dimension was
187 defined as the amount of RSQ for the 1D explanation to evaluate the perceptual significance of each
188 dimension. The amount added in RSQ at a later dimension was taken as the weight for the next
189 dimensions. As a further step, we conducted Procrustes analysis using the *Procrustes.m* function of
190 MATLAB for both sets of points and performed a linear transformation (translation, reflection, and
191 orthogonal rotation) to map the spaces onto each other. The resulting normalized residual sum of
192 squared errors (*d-value*) represents the goodness-of-fit and provides a measure of congruency between
193 visual and tactile perceptual spaces. Because the MDS method generates relative positions in space
194 and not absolute positions, a linear transformation is a valid operation for this kind of data (Gaissert
195 and Wallraven, 2012). Thereafter, to test whether the two categories of objects were represented in the
196 brain as two distinct categories for visual and tactile modalities, the Euclidean distances between pairs
197 of objects within each category and between pairs of objects between different categories were
198 calculated.

199 **3D shape features extraction and selection**

200 According to our stimulus generation algorithm and questionnaires, shape features play an essential
201 role in rating the similarity between object pairs. Thus, in our second analysis, we investigated which

202 object features were used to create compatible perceptual spaces for the visual and tactile sensory
203 modalities. First, all 16 digital embryos were aligned to a similar orientation. The iterative closest
204 point (ICP) algorithm is applied to align objects. The ICP algorithm iteratively applies transformations
205 (a combination of translation and rotation) to minimize square errors between corresponding objects
206 (Besl and McKay, 1992; Chen and Medioni, 1991). For further analysis, we extracted 17 relevant
207 shape features from all 16 aligned digital embryos (Table1). The Euclidean distance between the pairs
208 of objects for each shape feature was calculated to generate the computational dissimilarity measures.

209 In line with the results of the questionnaires, one important feature was the curvature of the objects.
210 Because the objects are basically meshes formed by triangles, the Gaussian curvature (F1) at each
211 vertex was calculated by computing the curvature tensor and the principal curvatures at each vertex of
212 a digital embryo (Rusinkiewicz, 2004; Shum et al., 1996). Differences between the curvature of each
213 mesh's vertex for all pairs of objects were calculated to perform a shape dissimilarity matrix based on
214 curvature. The Euclidean distances from all vertices to the center of an object (F2) provide additional
215 information about the global curvatures. The surface area (F3) and volume (F4) of an object indicate
216 its size. The different views of an object contain sufficient information about the shape (F5-F10). 2D
217 projections provide 2D perspectives of the variance of an object. The 2D projection to the XY, YZ,
218 and XZ planes gives a perspective view from the top, lateral, and frontal sides of the object,
219 respectively. Geometric measures represent the geometric properties of an object, such as size, shape,
220 angle, position, and dimension. The size and diagonal of the smallest enclosing bounding box illustrate
221 the size, volume, pattern of branches, and number of branches (F11-F12).

222 The mass distribution provides information about the patterning of the branches of the objects. One
223 possible way to describe the mass distribution in a rigid body is the inertia tensor (F13). Previous
224 studies have identified the informational value of the inertia tensor in the tactile perception of object
225 properties (Cabe, 2019; Carello et al., 1996; Kingma et al., 2002; Pagano et al., 1994). The
226 eigenvalues of the inertia tensor or principal axis (F14) have been shown to be related to the
227 perception of an object's shape, length, width, height, and heaviness. The eigenvectors of the inertia
228 tensor or moments of inertia tensor (F15) are related to the perception of an object's orientation and
229 grasp position (Kingma et al., 2002). To analyze all geometric measures, we used the 3D mesh
230 processing system Meshlab_64bit (<https://www.meshlab.net/>) (Cignoni et al., 2008). Furthermore, we
231 used the number of triangles (F17) that formed the digital embryos as a relevant feature for the visual
232 and tactile system. Based on the process of the algorithm for generating digital embryos, when fission
233 proceeds, a triangle is split into four new triangles, indicating that the number of vertices increases. If
234 these vertices are independent, they will move about in space according to the force applied to them.
235 From this we concluded that more vertices leads to more tiny concavity and convexity on the objects.
236 These tiny bumps could refer to surface quality or texture and they are comprehensible for tactile
237 sense and even for visual sense.

238 To evaluate each single feature validity, we defined two criteria. The first criterion was defined as the
239 mean d-value in fitting the physical map derived from each feature to all individual subject maps
240 (single-fitting error). The second criterion was the mean d-value in fitting each individual map to all
241 other individual maps (cross-fitting error). Cross-fitting error defines how well individual subject
242 maps are fit to each other. If the single-fitting error generated by each feature and the cross-fitting
243 error are not significantly different, it could be considered that the feature fits the human data well
244 (Cooke et al., 2006, 2005a). To test perceptual validity, we performed a two-tailed t-test between
245 single-fitting and cross-fitting errors (corrected for multiple comparison).

246 Further, given that a combination of different features reconstructs a different perceptual space, and in
247 this study, the combination of features plays a role, we performed perceptual validity analysis on the
248 combination of features as well. We evaluated all combinations of features listed in Table 2.
249 Comparing the mean d-value in fitting a physical map derived from each combination to all individual
250 maps (combination fitting error) with the mean d-value in fitting each individual map to all other
251 individual maps (cross-fitting error).

252 To assess which combination of features forms highly similar veridical spaces in human visual and
253 tactile perception, different combinations of features were tested to create different physical spaces.
254 There are 131,071 different combinations, ranging from a single feature to combinations of 17 features
255 (${}_{17}C_1+{}_{17}C_2+{}_{17}C_3+\dots+{}_{17}C_{16}+{}_{17}C_{17}=2^{17}-1$). The physical space for each combination was created by
256 applying an MDS analysis to the dissimilarity matrix obtained from the pair-wise distances of features.
257 For example, there are 136 (${}_{17}C_2$) different combinations of two features (F1-F2, F1-F3, ..., F16-F17).
258 After normalizing the pairwise distance of each feature, an MDS analysis was applied to the average
259 of two normalized distances of the corresponding features to form physical spaces. To evaluate the
260 validity of the perceptual space, the goodness-of-fit criterion (d-value) as a linear transformation
261 (translation, reflection, and orthogonal rotation) was applied to assess the map fitting between physical
262 spaces and the visual and tactile perceptual space. A feature combination of F2 and F13 resulted in
263 highly similar physical and visual perceptual spaces – i.e., best fit of the visual perceptual spaces to the
264 physical space was achieved using the combination of the distances from all vertices to the center of
265 the object and its inertia tensor. We repeated these steps for both modalities to calculate the d-values
266 for all possible feature combinations.

267 **Results**

268 **Visual and tactile perceptual spaces**

269 One group of 25 participants underwent the similarity judgment experiment in the visual modality,
270 while another participated in the tactile modality. The average similarity matrices across all
271 participants are shown in Figure 2. We observed a high correlation ($r = 0.82, P < 0.001$) between

272 the visual and tactile similarity matrices, which indicates an equal interpretation of object similarities
273 for both modalities. Using the average dissimilarity matrices, we ran an MDS analysis to calculate the
274 stress values for one to ten dimensions for both modalities (Figure 3A).

275 To select the number of sufficient dimensions for our similarity data, we applied the statistical elbow
276 method. Because human data mostly contain noise, stress values of zero are not observed in empirical
277 data; moreover, the lower the stress value, the higher the data dimensionality. Several studies have
278 shown that a stress value of less than 0.2 is sufficient to describe human data faithfully (Clarke and
279 Warwick, 2001; Cooke et al., 2007; Gaißert et al., 2008). The elbow in the stress plot was visible in
280 two or three dimensions (Figure 3A). Given that the stress values for all dimensions were less than 0.2,
281 one dimension was also sufficient to visualize perceptual spaces, although the elbow in the stress plot
282 was visible in two or three dimensions. Furthermore, the mean weight for the first dimension across
283 visual group was 0.958, while the mean weight of the second and the third dimension were 0.018 and
284 0.015, respectively. Similarly, in the tactile group, the weight of the first dimension was 0.897 and the
285 mean weights of the second and the third dimension were 0.0629 and 0.0256. These results not only
286 prove again the higher importance of the first dimension for the visual and tactile modality, but also
287 demonstrate that the second and third dimensions play a minor role in the data interpretation. Here, for
288 better visualization, we plotted the visual and tactile perceptual spaces for two dimensions, although
289 the second dimension was of little importance in information reconstruction. The MDS output for two
290 dimensions for both modalities (Figure 3B, C, and Figure 3-1) showed highly similar perceptual
291 spaces across the visual and tactile modalities ($d=0.136$, zero indicates perfect alignment). These
292 results indicate that, in the absence of visual perception, tactile inspection is capable of reconstructing
293 the same perceptual space as the visual system, and vice versa, even for unfamiliar objects.

294 In addition to the highly congruent perceptual spaces of visual and tactile exploration, the two clusters
295 represent the two object categories of the VP algorithm. Here it is important to point out that the
296 participants were not aware of any of the categories to which the objects belonged. For further
297 analysis, we investigated the degree of cluster definition in both perceptual spaces by measuring the
298 Euclidean distances between pairs of objects within a category and pairs of objects between categories.
299 The results indicate a significant difference between within-category distances and between-category
300 distances (Visual: $t(118) = 23.1$, $p < 0.0001$; Tactile: $t(118) = 15.4$, $p < 0.0001$; Figure 4).

301 **Perceptual validation of computational features**

302 The observed similarity between visual and tactile perceptual spaces raises the question of which
303 stimulus features contribute to the formation of these highly congruent perceptual spaces.

304 The average volume of objects within category one and two were $8.02 (\pm 0.45) \times 8.65 (\pm 0.24) \times 5.39$
305 $(\pm 0.21) \text{ cm}^3$ and $8.21 (\pm 0.32) \times 8.76 (\pm 0.48) \times 5.44 (\pm 0.20) \text{ cm}^3$, respectively. There was no

306 significant difference in the length ($t(7) = 0.9167$, $p = 0.3898$), width ($t(7) = 0.4489$, $p = 0.6671$), or
307 height of objects between the two categories ($t(7) = 0.5706$, $p = 0.5861$). The average weight of
308 objects within categories one and two were 13.62 ± 0.52 g and 13.5 ± 0.53 g, respectively. There was
309 no significant difference between the weight of objects in both categories ($t(7) = 0.4237$, $p = 0.6845$).
310 Therefore, object features such as weight and size do not contribute to object categorization. In
311 contrast, shape features, such as the number of branches, size, and pattern, play a major role in object
312 categorization, as shown by our questionnaire results (Figure 5).

313 As can be seen in Table 2, visual and tactile modalities share six common features: the distances from
314 all vertices to the center of objects (F2), the volume of objects (F4), the area of the projection of the
315 object to XY-plane (F5), bounding box size (F11), inertia tensor (F13), and axis momenta (F15).
316 Referring to the surface texture of the objects, the number of triangles (F17) plays a major role in the
317 tactile modality. Four features exclusive to the visual modality include Gaussian curvatures of objects
318 (F1), the area of the projection of the object to the XZ-plane (F7), the distances of the center from
319 edges on the XY-projection (F8), and principal axes(F14).

320 To find relevant features, we calculated the physical space for each possible feature combination (1 to
321 17 features) using the MDS method. The goodness of fit criterion (d-value) was calculated between all
322 physical spaces and the visual or tactile perceptual spaces: i.e., the higher the fit, the lower the d-value.
323 The minimum d-values are listed in Table 2.

324 In fitting to the human visual/tactile map, single-fitting error differed significantly from the mean
325 cross-fitting error. Note, although single-fitting errors provided a poor fit ($P < 0.001$) (Figure 6A),
326 combination fitting errors provided better fits (Figure 6B). Our results indicate that some features of
327 an object may not be meaningful on their own, but their combination creates a meaningful feature that
328 leads to the correct perception of an object. There are several feature combinations that are statistically
329 close to human perceptual maps. Since these combinations share several common features, we decided
330 to focus only on the combination of features which caused the absolute minimum d-value to make the
331 comparison between visual and tactical modalities possible (See Discussion).

332 A physical space derived from a combination of ten features showed the best similar fit (minimum d-
333 value, $d = 0.048$) to the mean perceptual space derived from the human visual system. Moreover,
334 comparing physical spaces derived from a combination of features to the stimulus space derived from
335 human tactile perception showed that a combination of seven features constructed a physical space
336 with the minimum d-value ($d = 0.101$). These findings demonstrate that participants use multiple
337 rather than single features in their perceptions. On the other hand, visual and tactile sensory systems
338 share common features in object identification.

339 Discussion

340 The current study addressed the role of shape features that mediate the interchangeability between
341 visual and tactile modalities. To this end, we generated a set of complex, natural digital embryos (3D
342 objects) based on a VP algorithm that simulates the biological process of embryogenesis. These 3D
343 objects were used to perform similarity rating experiments using visual and tactile modalities. One
344 objective of the current study was to provide a more realistic situation in which participants were
345 confronted with the perception of 3D objects, while minimizing tactile influences during active visual
346 exploration and eliminating the influence of the experimenter. Moreover, neuroimaging studies
347 demonstrated that the cortical mechanisms of three-dimensional (3D) shape processing are different in
348 vision and touch, while cortical mechanisms of two-dimensional form are similar (Hsiao et al., 2008).
349 Hence, in order to implement the goals mentioned, the visual experiment used VR technology to
350 enable active and unconstrained visual exploration without additional tactile information. In the tactile
351 experiment, subjects explored the same objects as 3D plastic printouts while being blindfolded.
352 Overall, we showed highly congruent visual and tactile perceptual spaces that are most likely based on
353 shared common features between the spaces.

354 Seminal studies demonstrate that tactile and visual sensory systems are both accurate in shape
355 discrimination. Visual perception is based on parallel processing of transforming light from our 3D
356 environment into a two-dimensional retinal image, while tactile perception is serially developed
357 through an exploratory procedure on 3D objects (Gaißert et al., 2010a; Klatzky and Lederman, 2011).
358 In our study, object differences were computed using seventeen 2D and 3D features. Curvature is one
359 of the important features which has been shown play an important role for visual and tactile
360 perceptions (Barth et al., 1998; Lim and Charles Leek, 2012; Pont et al., 1997). Curvature information
361 plays a particularly important role to provide the three-dimensional information of the surface
362 structure of an object (Strother et al., 2015; Todd, 2004; Yue et al., 2020). fMRI studies of monkeys
363 and humans demonstrated that the temporal cortex and retinotopic regions of the visual system are
364 involved in processing of curvature information (Yue et al., 2020). However, curvature information is
365 processed by cutaneous receptors in tactile system (Kappers, 2011) to judge the differences between
366 objects. Furthermore, the front and back view of objects are more informative in the visual and touch
367 system, respectively (Newell et al., 2001). Our results revealed that frontal and top/back views played
368 a role in visual exploration and top/back views played a role in tactile exploration, consistent with
369 findings by Newell et al. (2001). In addition, the mass, center of mass, and the inertia tensor are an
370 important set of physical properties for visual and tactile perceptions. They describe the mass
371 distribution, object's weight, and resistance to motion changes during viewing or manipulating an
372 object. Humans are able to perceive elements of the inertia tensor of the held objects through dynamic
373 touch, which is a simulation mechanism of muscular sensitivity to the inertia parameters (Casati and
374 Pasquinelli, 2005; Fitzpatrick et al., 1994; Mavrakakis and Stolkin, 2020).

375 Among these common features, participants relied on inertia tensor information both during tactile
376 exploration and visual inspection. While several studies have proven the role of inertia tensor in tactile
377 perception (Cabe, 2019; Carello et al., 1996; Kingma et al., 2002; Pagano et al., 1994), the role of
378 proprioceptive features in visual perception is unclear. The integration of perception with active
379 exploration, however, offers a possible explanation: When participants explore an object in a VR
380 environment using a controller, they are able to change the object orientation without any restriction to
381 view objects from all sides; hence, they can collect inertia information, such as the object's length,
382 width, height, and mass distribution, while rotating their wrists to control the orientation of objects.
383 Taken together, our results suggest that the inertia tensor plays a role in visual and tactile perception if
384 humans explore objects in a natural, active manner for similarity judgments and object identification.
385 In addition, global features related to the size and volume (F2, F4, and F11) contributed to both
386 modalities: by viewing and grasping objects with the hands, these features can be obtained from any
387 object. Furthermore, the top view of the objects (F5) contained relevant information for both the visual
388 and tactile senses. Because the top view of objects presents the largest surface area, it may provide
389 more information about the shape of objects.

390 In contrast, some features were exclusive to the visual or tactile systems. The Gaussian curvature
391 feature (F1), which describes the convexity and concavity of an object at the vertices, only played a
392 role in visual perception. This finding may be attributed to the following: when humans explore an
393 object, the overall convexness and concaveness of the object can be perceived literally at first glance
394 by the visual system, whereas the fingertips gather only limited curvature information related to those
395 parts of an object that are actually touched; therefore, obtaining curvature features by touch requires a
396 much higher sample rate. On the contrary, as a feature that only contributes to the tactile modality, the
397 number of triangles contained in the 3D objects describes the surface roughness, i.e., its texture.
398 Texture and shape are of equal importance during tactile conditions (Cooke et al., 2007, 2005b).
399 Notably, cell division during embryo generation caused tiny variations in object texture, which may be
400 easily recognized by the tactile system. We sanded the surfaces of all plastic objects to minimize this
401 effect but given the importance of texture in the tactile modality, even the smallest deviations between
402 objects may provide relevant information. Cooke et al. (2005a, 2005b, 2006) established a high-level
403 approach to validate the extracted physical features by comparing behavioral perceptual spaces with
404 physical spaces derived from computational measures. They extracted 6 features in the first study and
405 eight features in the second. Half of the features were 2D features and related to gray-values between
406 objects. Other features were extracted from a 3D mesh, such as object perimeter and curvature. In
407 general, they tested single features to validate the physical space of a computational measure.
408 However, in real life the combination of several features guides humans object recognition. For
409 instance, to identify a walnut, a pecan, a plum, and a cherry, relying only on the perimeter helps
410 identifying the cherry. If we pay attention to bumpiness, softness, and perimeter simultaneously, it is
411 possible to identify all of these objects accurately. To close this gap, in the current study, seventeen

412 features from a 3D mesh were extracted. We extracted seventeen features from different modalities to
413 better describe the physical properties of objects using both visual and tactile modalities. However, in
414 our study, features were extracted from 3D mesh, not from 2D photographs. The extracted features
415 describe the three-dimensional nature of objects and are similarly comprehensible for both visual and
416 tactile senses. These features mainly describe the shape of objects. Most importantly, high-level and
417 abstract features that participants are not capable of describing easily have been ignored. In addition to
418 single feature comparisons, we used different feature combinations to detect the optimal combination
419 to describe the perceptual space of various modalities.

420 Several feature combinations play a role to reconstruct human perceptual spaces in visual and tactile
421 modalities. Although we only focused on the feature combination that caused the absolute minimum
422 d-value, selecting other feature combinations in the same range would not contradict the finding of the
423 current research. With a brief reflection on the results (Figure 6 and Table 2), it is obvious that even
424 nonsignificant feature combination maps share common features which can reconstruct visual and
425 tactile human perceptual maps. For instance, the distances from all vertices to the center of objects
426 (F2) is an important feature that plays a major role in visual and tactile representation regardless of
427 which combination is chosen. This feature provides some information about global shape, mass
428 distribution, and pattern of branches. The surface area (F3), the volume of objects (F4), and bounding
429 box size (F11) are other features that are mostly involved in both modalities. These features are
430 recognizable by both senses and they describe shape objects as well. The top/back view of the objects
431 (F5) is also a relevant feature that in combination with other features leads to the perception and
432 identification of objects. Inertia tensor (F13-F15) as a physical-mechanical description of object
433 properties is associated with the perception of an object's shape, length, width, height, heaviness,
434 object's orientation, and grasp position. In order to choose the same criterion for comparing the visual
435 and tactile spaces, considering that a low d-value close to zero indicates a better fit, we chose the
436 combination with the absolute minimum d-value in both modalities to represent human perceptual
437 maps.

438 Overall, our findings raise the question of how the brain uses shape information from two different
439 modalities to form highly congruent perceptual spaces. Conceivably, the brain can form a multimodal
440 perceptual space for relevant features, which is the object shape. This multimodal perceptual space is
441 accessible to both modalities. For example, if a person is trained to categorize objects based on shape
442 variations either visually or tactually, he or she can categorize novel objects using visual or tactile
443 information even in the absence of trained sensory cues (Wallraven et al., 2014; Yildirim and Jacobs,
444 2013). This is presumably because a shared multisensory representation integrates the sensory
445 information of the shape independent of the input modality. Corroborating this assumption, many
446 neuroimaging studies on multisensory perception emphasize a common neural substrate in visual and
447 tactile shape processing (Amedi et al., 2001; Drucker and Aguirre, 2009; Lee Masson et al., 2016; Op

448 De Beeck et al., 2008). Amedi et al. found a region within the human lateral occipital complex (LOC)
449 that is activated during multimodal object perception (Amedi et al., 2001). More recently, Masson et
450 al. showed that the lateral occipital cortex, as a multisensory convergence area, becomes activated
451 during visual and tactile shape processing (Lee Masson et al., 2016). These findings implicate the
452 LOC as a candidate region to encode the multimodal perceptual space of shape processing
453 independent of modalities (Lacey et al., 2009). The existence of such a multimodal perceptual
454 mechanism might be the main reason why humans can interchangeably use visual and tactile
455 modalities because the acquired object information can be shared or transferred between modalities.

456 The sharing of certain common features among sensory inputs is a prerequisite for the integration of
457 sensory information from different modalities (Holmes et al., 2008). Physically, the adequate stimuli
458 and perception of photoreceptors and mechanoreceptors differ significantly from each other.
459 Nevertheless, they both provide detailed and congruent information about the perceptual space.
460 Learning, in particular categorization, can have a strong influence on the dimensionalization of
461 complex objects (Palmeri et al., 2004). Although previous studies used a parametrically defined
462 complex object space to determine whether the tactile and visual modalities are capable of forming a
463 veridical perceptual space (Gaißert et al., 2010b, 2008; Lee Masson et al., 2016), the brain does not
464 necessarily need to use all given dimensions (i.e., object features) to represent the perceptual spaces.
465 The visual system might rely on a limited number of independent shape features to distinguish the
466 shape of objects between categories (Op de Beeck et al., 2003; Ullman et al., 2002). During visual
467 object exploration, only the relevant features are enhanced, and irrelevant features are suppressed.
468 Because the tactile perceptual system has much in common with the visual system (Cooke et al., 2007;
469 Gaißert et al., 2011, 2010a, 2008; Lacey and Sathian, 2014), it can be assumed that shape exploration
470 in the tactile system also uses only a limited number of dimensions. In our investigation, different
471 combinations of extracted features were used to find informative shape features that constructed two
472 veridical physical spaces akin to the visual and tactile perceptual spaces. Our results indicate that a
473 combination of ten features forms a physical space with maximal similarity to the visual perceptual
474 space, whereas a combination of seven features was capable of describing a physical space that is
475 highly similar to the tactile perceptual space. Based on d-values in the Table 2, the plot of d-values of
476 all possible combinations when fitting the visual and tactile perceptual spaces with the physical map
477 demonstrates a U-shape curve (See Extended Data Table 2-1). This U-shape curve demonstrated that a
478 single feature / a combination of a few features led to high d-values, and when the number of involved
479 features rose, the d-values again increased. This is consistent with the notion that not only humans use
480 multiple rather than single features in their perceptions but also they do not necessarily need to use all
481 given dimensions (i.e., object features) to represent the perceptual spaces (Ullman et al., 2002; Cooke
482 et al., 2007; Lacey et al., 2014). This finding shows that relying on a set of fixed dimensions might
483 facilitate the transfer of knowledge across modalities.

484 Categorization is an essential ability of the human brain, as it enables the organism to interact with its
485 surroundings in such a way as to ensure survival in a dangerous environment. While several models
486 describe human categorization behavior – e.g., the prototype theory, exemplar theory, and decision
487 bound theory (Ashby and Maddox, 2011)– they all share a common feature between them: namely, the
488 similarity of objects. Therefore, similarity is a key component in identifying and categorizing new
489 objects (Gaißert et al., 2011). In our current study, perceptual spaces revealed clear object clusters
490 based on similarity, despite the participants having no prior knowledge of the objects’ categories.
491 Shepard et al. (Shepard, 2001) have proposed that objects from the same category should be locally
492 close in perceptual spaces. Our results reveal that clusters within perceptual spaces correspond to
493 different object categories. Furthermore, research by Edelman (Edelman, 1999) claimed that objects
494 from the same category should be represented in perceptual spaces within a single cluster. Our results
495 demonstrated that the distance was lower for pairs of objects with greater similarity (i.e., same
496 category) and higher for pairs of objects with less similarity (i.e., different categories, Figure 4). The
497 role of similarity in forming the basis of perceptual categorization and the role of shape in the
498 formation of category structure has been controversial for a long time among cognitive neuroscientists
499 (Moore, 2002). Our results support previous findings that similarity plays an important role in
500 categorization.

501 However, in our study, a VP algorithm was used to create a unique set of novel, naturalistic 3D objects
502 and to avoid possible confounds or special cases in object shapes. This algorithm benefits from the
503 independent creation of shape variations within and across generated categories that were not imposed
504 by an experimenter. In addition, the features of digital embryos are very similar to those of natural
505 objects. While these stimuli provide a rich set of objects to investigate the scientific questions, there is
506 no underlying parameter space to identify and control the dimensionality of digital embryos. This
507 limits restoring the dimensionality of the physical objects from the MDS output. Given that the
508 purpose of the current study was to create naturalistic object categories that differ only in shape, the
509 VP algorithm made it possible to design our desired objects.

510 Further, to demonstrate that our methods are reliable on other stimuli sets, four different random
511 categories sets were created using a VP algorithm. Figure 7 reveals that our methods were able to
512 discriminate all different categories well.

513 Taken together, our results indicate a link between perceptual spaces of visual and tactile systems,
514 which suggests that both modalities use a similar cognitive process to represent shape information.
515 Elucidating these interactions between modalities could help to advance understanding of how humans
516 can interchangeably use different modalities to interact with their surroundings.

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664 **Figure Captions**

665 **Figure 1.** Stimuli generation and task designs. **A**, Generating object categories using a virtual
666 phylogenesis algorithm starting from an icosahedron. At each generation G_n , selected embryos procreate, leading
667 to generation G_{n+1} . Simulated embryonic development processes were applied to a given parent object from G_2
668 (circles) to generate two classes of novel objects in G_3 : eight G_3 -siblings from one parent formed a distinct
669 object category. In total, two object categories from the third generation served as stimuli for the current study,
670 with siblings 1-8 numbered by the experimenter accordingly within each category. The subjects were unaware of
671 how the digital embryos were generated and/or categorized. **B**, The virtual office was furnished with a desk,
672 which was located in front of the participants. If the participants looked towards their left, bookshelves, a printer,
673 some books, and a monitor on a study table were visible; towards their right, there was a window with a view of
674 the outside. **C**, Visual similarity task using virtual reality technology. **D**, Tactile similarity experiment using 3D
675 tangible objects generated by a 3D printer. The objects were printed out with two different colors in order to be
676 more recognizable for the experimenter. Since participants were unable to see the objects, this color difference
677 did not affect the experimental results.

678 **Figure 2.** Similarity matrices. **A**, Average group similarity matrix for visual similarity judgment. **B**,
679 Average group similarity matrix for tactile similarity judgment. The color codes for the similarity ratings
680 corresponded to the numbers, ranging from 1 (dissimilar, dark blue) to 7 (identical, dark red). Numbers on the x-
681 and y-axes refer to the digital embryos in each category (8 objects per category) according to Figure 1A.

682 **Figure 3.** Two-dimensional visual and tactile perceptual spaces. **A**, The stress values for both modalities
683 were calculated for one to ten dimensions. The elbow indicates that two data dimensions are sufficient to explain
684 the visual and the tactile perceptual space. **B**, Two-dimensional visual perceptual space (See Extended
685 Data Figure 3-1A, C for one- and three-dimensional visual perceptual spaces). **C**, Two-dimensional tactile
686 perceptual space (See Extended Data Figure 3-1B, D for one- and three-dimensional tactile perceptual spaces).
687 The numbers refer to the object numbers in each category according to Figure 1A. Contrast level codes different
688 categories; black: category 1 and gray: category 2

689 **Figure 4.** Euclidian distance. The average distance between pairs of objects within a category (black
690 bars) is significantly smaller than the distance between pairs of objects from different categories (gray bars) for
691 both modalities. Error bars represent the standard error of the mean (SEM). ** means $p < 0.0001$

692 **Figure 5.** Questionnaires. At the end of each similarity judgment test, participants were asked to rate the
693 importance of features to determine which features played the main role in their similarity judgments. In addition
694 to the weight, color, material, global patterning, texture, we listed further details describing the shape of digital
695 embryos: branch size, branch pattern, number of branches, global shape, and curvature. The results for both
696 modalities indicated that the shape features played a major role. Features such as weight, size, and the pattern of
697 branch distributions were significantly more important for the tactile similarity judgment experiment than for the
698 visual. Bars represent the mean ratings across all participants over the visual (gray) and tactile (black) modality
699 (0 means no importance and 6 means very important). Error bars represent the standard error of the mean (SEM).
700 An asterisk* indicates $p < 0.01$.

701 **Figure 6.** Mean d-values (Procrustes Fit Error). A, Fits between computational measures of a single
702 features with visual and tactile maps. B, Fits between computational measures of a combination of features with
703 visual and tactile maps. F1-F17 indicate the number of single features. N1-N17 presents combination of features
704 listed in Table 2. Asterisks demonstrate that a reconstructed map of a feature or combination of features is
705 significantly different from perception in human behavior ($p < 0.01$).

706 **Figure 7.** The average distance for five different sets. The average distances between pairs of objects
707 within and between pairs of objects for five different sets of objects. Within category (black bars) and between
708 categories (gray bars). Error bars represent the standard error of the mean (SEM). ** means $p < 0.0001$

709 **Figure Captions of the Extended Data**

710 **Table 2-1.** The d-values in Table 2 show that visual and tactile d-values lead to U-shape curves. A single
711 feature or a combination of a few features led to high d-values, and when the number of involving features rose,
712 the d-values again increased. It supports the notion that humans do not necessarily need to use all given features
713 to reconstruct the perceptual spaces.

714 **Figure 3-1.** One and three-dimensional visual and tactile perceptual spaces. A, One-dimensional visual
715 perceptual space. B, One-dimensional tactile perceptual space. C, Three-dimensional visual perceptual space. D,
716 Three-dimensional tactile perceptual space. The numbers refer to the object. Color codes two different
717 categories.

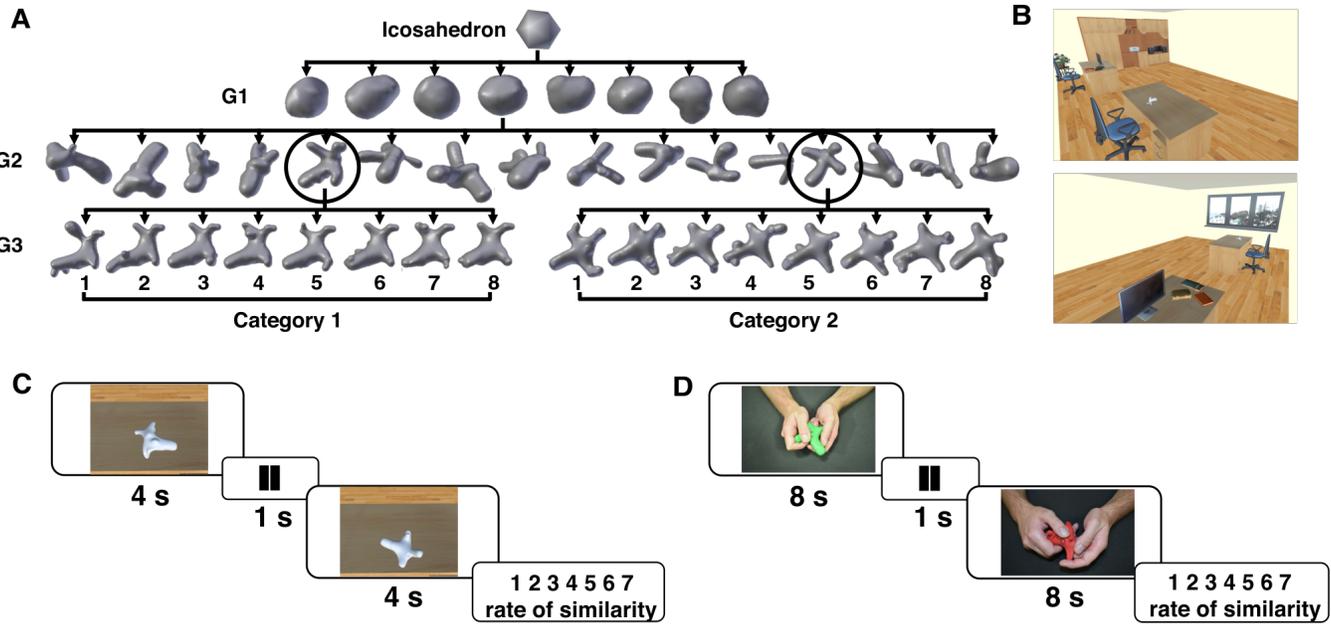
718 **Tables**

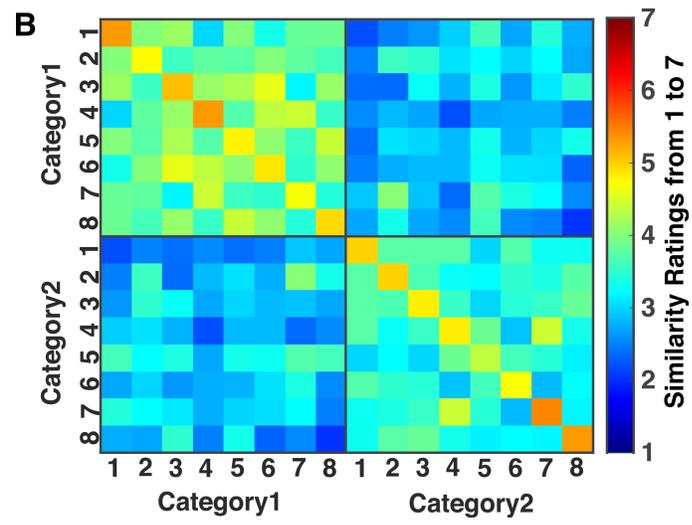
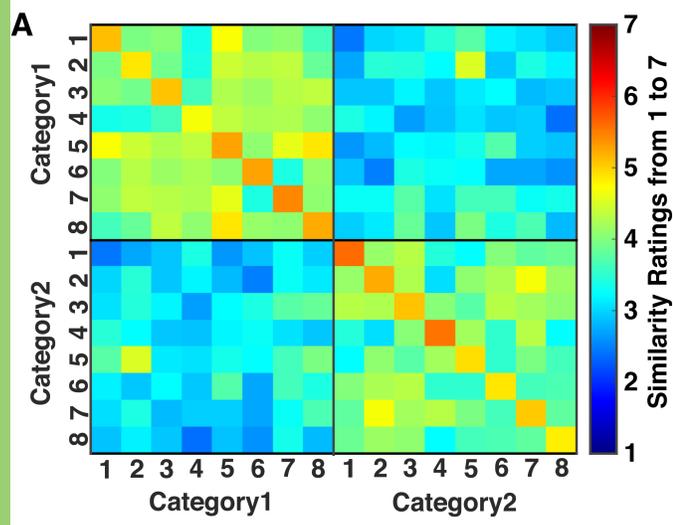
719 **Table 1.** Summary of the extracted features. The first and second columns illustrate 17 extracted shape
 720 features. The third column represents the selected feature that demonstrates the lowest d value between the
 721 physical and the visual perceptual spaces. The fourth column shows the selected features that lead to minimum
 722 d-value between physical and the tactile perceptual space.

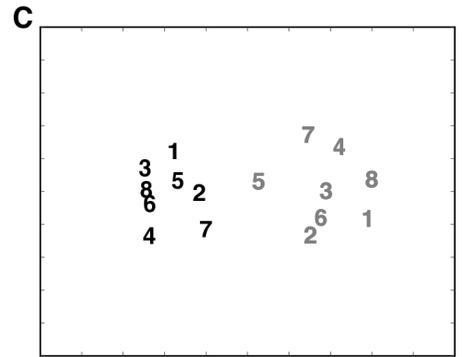
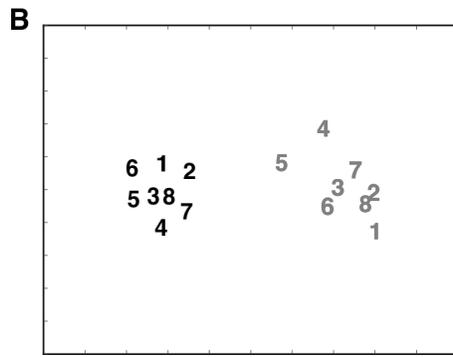
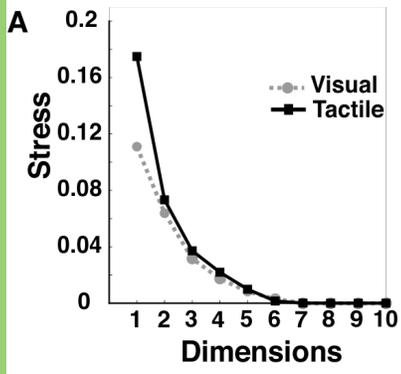
Feature	Definition	Visual modality	Tactile modality
F1	Gaussian curvatures of objects	✓	×
F2	The distances from all vertices to the center of objects	✓	✓
F3	The surface area of objects	×	×
F4	The volume of objects	✓	✓
F5	The area of the projection of the object to XY-plane (top/back view)	✓	✓
F6	The area of the projection of the object to YZ-plane (lateral view)	×	×
F7	The area of the projection of the object to XZ-plane (frontal view)	✓	×
F8	The distances of the center from edges on the XY-projection	✓	×
F9	The distances of the center from edges on the YZ-projection	×	×
F10	The distances of the center from edges on the XZ-projection	×	×
F11	Geometric measure: Bounding box size	✓	✓
F12	Geometric measure: Bounding box diagonal	×	×
F13	Geometric measure: Inertia tensor	✓	✓
F14	Geometric measure: Principal axes	✓	×
F15	Geometric measure: Axis momenta	✓	✓
F16	The center of objects	×	×
F17	Topological measure: The number of faces that constructed objects	×	✓

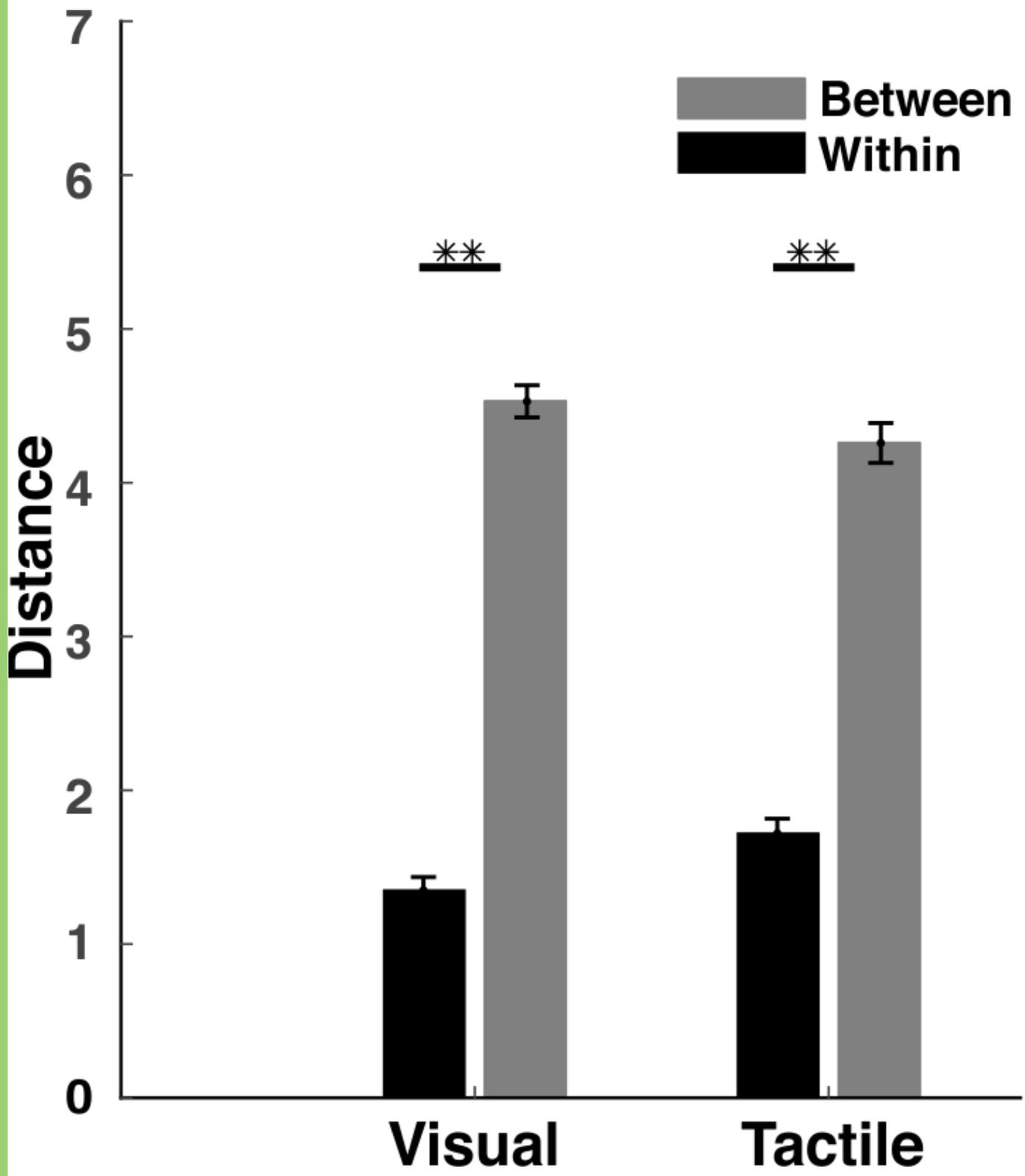
723 **Table 2.** The goodness of fit. The d values in the columns represent the minimum d values between the
 724 physical and the visual/tactile perceptual space for a different combination of features. The best fit quality
 725 between physical and visual perceptual spaces occurred when the ten features F1, F2, F4, F5, F7, F8, F11, F13,
 726 F14, F15 were selected. On the other hand, the combination of the seven features F2, F4, F5, F11, F13, F15, F17
 727 lead to the best fit quality between physical and tactile perceptual spaces. These two modalities share the features
 728 F2, F4, F5, F11, F13, F15. (See Extended Data Table 2-1)

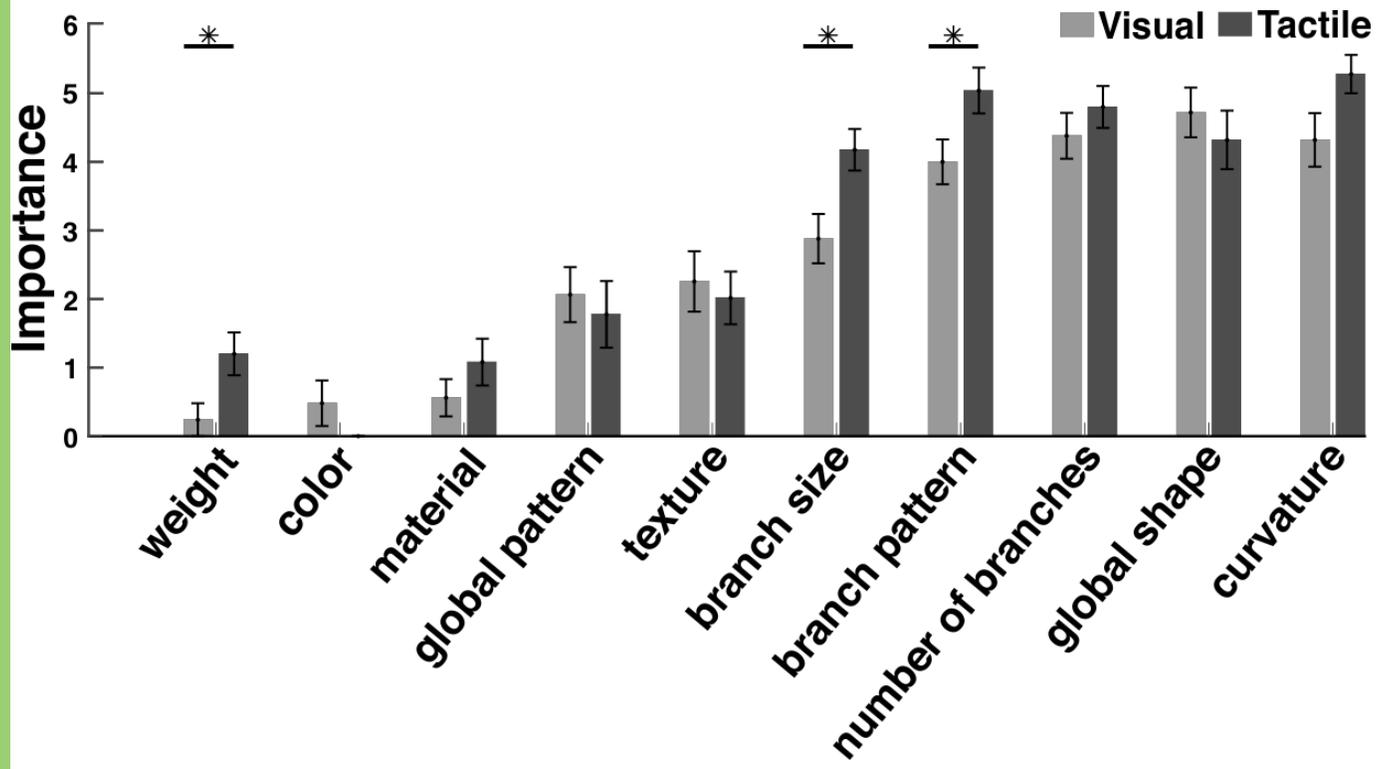
	N	Fit quality between physical and visual perceptual spaces	Fit quality between physical and tactile perceptual spaces
Minimum d-values for n-combination of features(N=1-17)	1	d=0.158 (F13)	d=0.266 (F13)
	2	d=0.120 (F2, F13)	d=0.215 (F2, F9)
	3	d=0.098 (F5, F13, F14)	d=0.158 (F2, F4, F13)
	4	d=0.072 (F2, F11, F13, F14)	d=0.135 (F2, F4, F11, F16)
	5	d=0.061 (F2, F5, F11, F13, F14)	d=0.126 (F2, F4, F9, F15, F17)
	6	d=0.062 (F2, F3, F6, F12, F14, F15)	d=0.118 (F2, F4, F5, F10, F11, F17)
	7	d=0.053 (F2, F5, F6, F11, F13, F14, F15)	d=0.101 (F2, F4, F5, F11, F13, F15, F17)
	8	d=0.052 (F2, F3, F4, F8, F11, F13, F14, F15)	d=0.110 (F2, F4, F5, F6, F9, F10, F11, F15)
	9	d=0.050 (F2, F4, F5, F6, F7, F11, F13, F14, F15)	d=0.116 (F2, F4, F7, F10, F11, F12, F13, F15, F16)
	10	d=0.048 (F1, F2, F4, F5, F7, F8, F11, F13, F14, F15)	d=0.120 (F2, F4, F5, F7, F9, F10, F11, F14, F15, F17)
	11	d=0.050 (F2, F4, F5, F6, F7, F10, F11, F12, F13, F14, F15)	d=0.132 (F2, F3, F4, F7, F9, F10, F11, F12, F14, F15, F16)
	12	d=0.060 (F1, F2, F4, F5, F7, F8, F10, F11, F12, F13, F14, F15)	d=0.145 (F2, F3, F4, F6, F7, F9, F10, F11, F12, F14, F15, F17)
	13	d=0.078 All features were selected except F6, F9, F12, F17	d=0.150 All features were selected except F1, F6, F8, F13
	14	d=0.110 All features were selected except F6, F16, F17	d=0.171 All features were selected except F5, F8, F13
	15	d=0.167 All features were selected except F10, F14	d=0.271 All features were selected except F10, F14
	16	d=0.168 All features were selected except F14	d=0.272 All features were selected except F14
	17	d=0.168 All features were selected	d=0.272 All features were selected











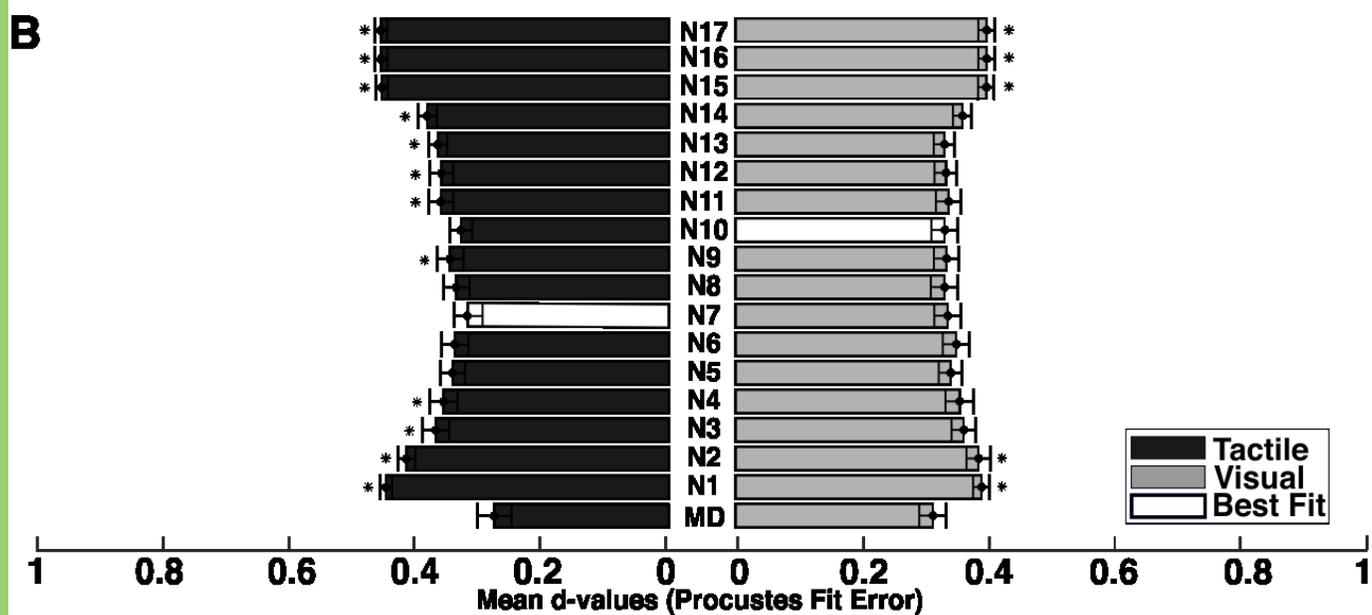
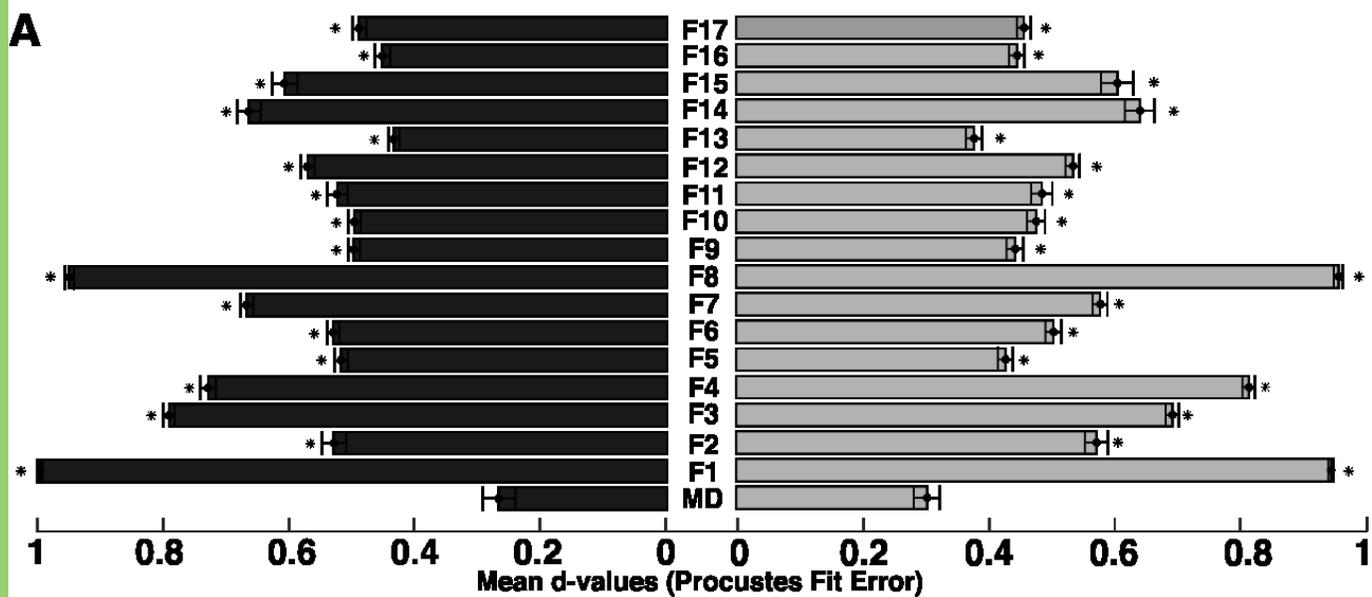




Table 1. Summary of the extracted features. The first and second columns illustrate 17 extracted shape features. The third column represents the selected feature that demonstrates the lowest d value between the physical and the visual perceptual spaces. The fourth column shows the selected features that lead to minimum d-value between physical and the tactile perceptual space.

Feature	Definition	Visual modality	Tactile modality
F1	Gaussian curvatures of objects	✓	×
F2	The distances from all vertices to the center of objects	✓	✓
F3	The surface area of objects	×	×
F4	The volume of objects	✓	✓
F5	The area of the projection of the object to XY-plane (top/back view)	✓	✓
F6	The area of the projection of the object to YZ-plane (lateral view)	×	×
F7	The area of the projection of the object to XZ-plane (frontal view)	✓	×
F8	The distances of the center from edges on the XY-projection	✓	×
F9	The distances of the center from edges on the YZ-projection	×	×
F10	The distances of the center from edges on the XZ-projection	×	×
F11	Geometric measure: Bounding box size	✓	✓
F12	Geometric measure: Bounding box diagonal	×	×
F13	Geometric measure: Inertia tensor	✓	✓
F14	Geometric measure: Principal axes	✓	×
F15	Geometric measure: Axis momenta	✓	✓
F16	The center of objects	×	×
F17	Topological measure: The number of faces that constructed objects	×	✓

Table 2. The goodness of fit. The d values in the columns represent the minimum d values between the physical and the visual/tactile perceptual space for a different combination of features. The best fit quality between physical and visual perceptual spaces occurred when the ten features F1, F2, F4, F5, F7, F8, F11, F13, F14, F15 were selected. On the other hand, the combination of the seven features F2, F4, F5, F11, F13, F15, F17 lead to the best fit quality between physical and tactile perceptual spaces. These two modalities share the features F2, F4, F5, F11, F13, F15. (See Extended Data Table 2-1)

	N	Fit quality between physical and visual perceptual spaces	Fit quality between physical and tactile perceptual spaces
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	6	d=0.062 (F2, F3, F6, F12, F14, F15)	d=0.118 (F2, F4, F5, F10, F11, F17)
	7	d=0.053 (F2, F5, F6, F11, F13, F14, F15)	d=0.101 (F2, F4, F5, F11, F13, F15, F17)
	8	d=0.052 (F2, F3, F4, F8, F11, F13, F14, F15)	d=0.110 (F2, F4, F5, F6, F9, F10, F11, F15)
	9	d=0.050 (F2, F4, F5, F6, F7, F11, F13, F14, F15)	d=0.116 (F2, F4, F7, F10, F11, F12, F13, F15, F16)
	10	d=0.048 (F1, F2, F4, F5, F7, F8, F11, F13, F14, F15)	d=0.120 (F2, F4, F5, F7, F9, F10, F11, F14, F15, F17)
	11	d=0.050 (F2, F4, F5, F6, F7, F10, F11, F12, F13, F14, F15)	d=0.132 (F2, F3, F4, F7, F9, F10, F11, F12, F14, F15, F16)
	12	d=0.060 (F1, F2, F4, F5, F7, F8, F10, F11, F12, F13, F14, F15)	d=0.145 (F2, F3, F4, F6, F7, F9, F10, F11, F12, F14, F15, F17)
	13	d=0.078 All features were selected except F6, F9, F12, F17	d=0.150 All features were selected except F1, F6, F8, F13
	14	d=0.110 All features were selected except F6, F16, F17	d=0.171 All features were selected except F5, F8, F13
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