
Research Article: New Research - Non-Double-Blind | Sensory and Motor Systems

Transition from Target to Gaze Coding in Primate Frontal Eye Field During Memory Delay and Memory-Motor Transformation

Visual-memory-motor transformations in FEF

Amirsaman Sajad^{1,2,3}, Morteza Sadeh^{1,3,4}, Xiaogang Yan¹, Hongying Wang¹ and John Douglas Crawford^{1,2,3,4,5}

¹Centre for Vision Research, York University, Toronto, Ontario M3J 1P3, Canada

²Neuroscience Graduate Diploma Program, York University, Toronto, Ontario M3J 1P3, Canada

³Department of Biology, York University, Toronto, Ontario M3J 1P3, Canada

⁴School of Kinesiology and Health Sciences, York University, Toronto, Ontario M3J 1P3, Canada

⁵Department of Psychology, York University, Toronto, Ontario M3J 1P3, Canada

DOI: 10.1523/ENEURO.0040-16.2016

Received: 25 February 2016

Accepted: 23 March 2016

Published: 5 April 2016

Funding: Canadian Institutes of Health Research (CIHR): MOP 130444. Ontario Graduate Scholarship; Queen Elizabeth II Scholarship; Provost Dissertation Award;

Conflict of Interest: Authors report no conflict of interests.

A.S. and J.D.C. designed research; A.S., M.S., X.Y., and H.W. performed research; A.S. analyzed data; A.S., M.S., X.Y., H.W., and J.D.C. wrote the paper.

Corresponding Author: Prof. J.D. Crawford, Centre for Vision Research, Room 0009A LAS, 4700 Keele Street, Toronto, Ontario M3J 1P3, Canada. Email: jdc@yorku.ca

Cite as: eNeuro 2016; 10.1523/ENEURO.0040-16.2016

Alerts: Sign up at eneuro.org/alerts to receive customized email alerts when the fully formatted version of this article is published.

Accepted manuscripts are peer-reviewed but have not been through the copyediting, formatting, or proofreading process.

This is an open-access article distributed under the terms of the Creative Commons Attribution 4.0 International (<http://creativecommons.org/licenses/by/4.0>), which permits unrestricted use, distribution and reproduction in any medium provided that the original work is properly attributed.

1 **Transition from Target to Gaze Coding in Primate Frontal Eye Field**
2 **During Memory Delay and Memory-Motor Transformation**

3 **Abbreviated Title:** visual-memory-motor transformations in FEF

4
5 **Authors:** Amirsaman Sajad¹⁻³, Morteza Sadeh^{1,3,4}, Xiaogang Yan¹, Hongying Wang¹,
6 and John Douglas Crawford¹⁻⁵

7 ¹Centre for Vision Research,
8 ²Neuroscience Graduate Diploma Program,
9 ³Department of Biology,
10 ⁴School of Kinesiology and Health Sciences,
11 ⁵Department of Psychology,
12 York University, Toronto, Ontario, Canada, M3J 1P3,

13
14 **Author Contributions:** AS and JDC designed research; AS, MS, XY, and HW
15 performed research; AS analyzed data; AS and JDC wrote paper; All reviewed paper.

16
17 **Corresponding Author:**

18 Name: Prof. J.D. Crawford
19 Address: Centre for Vision Research, Room 0009A LAS
20 4700 Keele Street, Toronto, Ontario, M3J 1P3;
21 Telephone: 416-7362100, ext: 88621
22 Email: jdc@yorku.ca

23
24 **Number of pages:** 71 (full manuscript, excluding title page)

25 **Number of Figures:** 11

26 **Number of words for Abstract:** 247

27 **Number of words for Significance Statement:** 119

28 **Number of words for Introduction:** 743

29 **Number of words for Discussion:** 1822

30
31 **Acknowledgements:** The authors thank Ms. S. Sun and Dr. Gerald Keith for computer
32 programming assistance, and Drs. S. Dash and R. Marino for editorial comments.

33
34 **Conflict of interest:** Authors report no conflict of interests

35
36 **Funding Sources:**

37 This study was supported by a grant from the Canadian Institutes for Health Research
38 to J.D. Crawford. J.D. Crawford was supported by the Canada Research Chair
39 Program. A. Sajad was supported by an Ontario Graduate Scholarship, a Queen
40 Elizabeth Scholarship, and a York Provost Dissertation Award. M. Sadeh was supported
41 by an Ontario Graduate Scholarship.

42 **Abstract**

43

44 The Frontal Eye Fields (FEF) participate in both working memory and sensorimotor
45 transformations for saccades, but their role in integrating these functions through time
46 remains unclear. Here, we tracked FEF spatial codes through time using a novel
47 analytic method applied to the classic memory-delay saccade task. Three-dimensional
48 recordings of head-unrestrained gaze shifts were made in two monkeys trained to make
49 gaze shifts toward briefly flashed targets after a variable delay (450-1500 ms). A
50 preliminary analysis of visual and motor response fields in 74 FEF neurons eliminated
51 most potential models for spatial coding at the neuron population level, as in our
52 previous study (Sajad et al., 2015). We then focused on the spatiotemporal transition
53 from an eye-centered target code (T ; preferred in the visual response) to an eye-
54 centered intended gaze position code (G ; preferred in the movement response) during
55 the memory delay interval. We treated neural population codes as a continuous
56 spatiotemporal variable by dividing the space spanning T and G into intermediate T - G
57 models and dividing the task into discrete steps through time. We found that FEF delay
58 activity, especially in visuomovement cells, progressively transitions from T through
59 intermediate T - G codes that approach, but do not reach, G . This was followed by a final
60 discrete transition from these intermediate T - G delay codes to a 'pure' G code in
61 movement cells without delay activity. These results demonstrate that FEF activity
62 undergoes a series of sensory-*memory*-motor transformations, including a dynamically
63 evolving spatial memory signal and an imperfect memory-to-motor transformation.

64 **Significance Statement**

65 Gaze-related signals in frontal cortex are often used as an experimental model for visual
66 working memory. However, the spatial codes employed during the delay between
67 target-related visual activity and intended gaze-related motor activity remain unknown.
68 Here, we show that frontal eye field delay activity (particularly in visuomovement
69 neurons) shows a progressive transition through intermediate target-gaze codes, with a
70 further jump to coding intended gaze position in movement neurons with no delay
71 response. Since our analytic method is based on fitting neural activity against variable
72 behavioral errors, this suggests that such errors accumulate during the memory delay,
73 and further escalate during the final memory-to-motor transformation. Any of these
74 vulnerable processes might be further degraded by diseases that affect frontal cortex.

75 **Introduction**

76 Primates routinely use remembered stimuli to guide spatial behavior, with varying
77 degrees of spatial precision (Gnadt et al., 1991; White et al., 1994). This could involve a
78 sensory-to-memory transformation, maintenance of the target in working memory, and a
79 memory-to-motor transformation (Goldman-Rakic, 1987; Postle, 2006; Bays et al.,
80 2011; Chatham and Badre, 2015). However, it is not known at what point in this
81 sequence the *spatial* code for the sensory stimulus is transformed into a spatial code for
82 movement, and likewise, when and how spatial errors in behavior arise (Gnadt et al.,
83 1991; Stanford and Sparks, 1994; Krappmann, 1998; Opris et al., 2003; Faisal et al.,
84 2008).

85 Memory-guided saccades provide an ideal experimental model for this question
86 because many saccade-related neurons in the brainstem and cortex exhibit spatially-
87 selective visual, memory, and / or movement responses (Funahashi et al., 1989; Bruce
88 and Goldberg, 1985; Schall, 2015; Wurtz et al., 2001). Further, the gaze control system,
89 which normally controls both eye and head motion, provides convenient parameters for
90 spatial coding (i.e., target, gaze, eye, head) in various egocentric frames (eyes, head, or
91 body) (Freedman and Sparks, 1997; Martinez-Trujillo et al., 2003; Sajad et al., 2015).
92 Still, a complete description of the spatiotemporal transformations in the sensory-
93 memory-motor transformation for gaze control remains elusive.

94 Neurophysiological studies often trained monkeys to look toward a location that is
95 spatially incongruent with the visual stimulus in order to dissociate target (*T*) coding in
96 visual responses vs. intended gaze position (*G*) coding in motor responses, without

97 addressing the intervening memory delay (Gottlieb and Goldberg, 1999; Everling and
98 Munoz, 2000; Sato and Schall, 2003). Most studies that explored this issue during delay
99 activity employed similar tasks to look for a discrete target-to-gaze switch (Funahashi et
100 al., 1993; Mazzoni et al., 1996; Zhang and Barash, 2004). Other studies showed a
101 gradual rotation of the population direction vector from the stimulus toward the
102 instructed movement direction in Dorsolateral Prefrontal Cortex (dlPFC), or a more
103 abrupt rotation in the mediodorsal thalamus (Takeda and Funahashi, 2004; Watanabe
104 et al., 2009). However, no previous experiment tested if delay activity evolves across
105 time through intermediate spatial codes (i.e., between T and G) in the visual-memory-
106 motor transformations for saccades *toward* remembered stimuli.

107 Assuming that one could track such codes through time, there are several ways that a
108 T - G transition could occur in memory-guided saccades (Fig. 1D). A sustained T code
109 followed by a late T - G transition would be compatible with sensory theories of working
110 memory (Funahashi et al., 1993; Constantinidis et al., 2001), whereas an early T - G
111 transition would be compatible with motor theories of working memory (Gnadt and
112 Andersen, 1988; Gaymard et al., 1999; Curtis and D'Esposito, 2006; Rainer et al.,
113 1999). Alternatively, T - G transition could progressively accumulate during the delay
114 (Gnadt et al., 1991; Wimmer et al., 2014). Another possibility (not shown) is that there is
115 no transition of coding *within* any given population of cells, but rather a temporal
116 transition of activity from a T -tuned population of neurons to a G -tuned population
117 (Takeda and Funahashi, 2007).

118 The monkey frontal eye fields (FEF), located in prefrontal cortex, are an ideal location to
119 study this question because they are directly involved in the sensorimotor

120 transformation for saccades and head-unrestrained gaze shifts (Bruce and Goldberg,
121 1985; Schall, 2015), and are part of the working memory network (Funahashi et al.,
122 1989; O'Sullivan et al., 1995; Dias and Segraves, 1999; Sommer and Wurtz, 2001). In a
123 recent study we exploited the variable behavior of head-unrestrained gaze shifts to
124 show that FEF visual and motor responses encode T and G respectively (both relative
125 to initial eye orientation) in saccades made toward remembered visual stimuli (Sajad et
126 al., 2015). However, this previous analysis could not show when or how this transition
127 happens, and did not explore the contributions of individual cell types. Here, we used a
128 similar approach, but applied our analysis in steps through time to fit a continuum of
129 intermediate T - G models through the entire course of a memory-guided saccade task.
130 Since this method is based on fitting spatial models against variable behavior such as
131 errors in final gaze direction (Keith et al., 2009; Sajad et al., 2015), this also provided a
132 direct measure of how such errors accumulate through different phases of a memory-
133 guided gaze shift. Further, with the use of a larger data set, we were able to categorize
134 our cells into different memory (or non-memory) related populations, in order to
135 understand their differential contributions through time to the T - G transition.

136 **Materials and Methods**

137 *Surgical procedures, identification of FEF, and behavioral data recordings*

138 All protocols were in accordance with the Canadian Council on Animal Care guidelines
139 on the use of laboratory animals and approved by the York University Animal Care
140 Committee. The data were collected from two female *Macaca mulatta* monkeys
141 (monkeys A and S). Each animal underwent surgeries for implanting the recording
142 chamber (19mm diameter) which was centered in stereotaxic coordinates at 25mm
143 anterior for both monkeys, and 19mm for one and 20mm lateral for the other. A
144 recording chamber was attached over the trephination with dental acrylic (Fig. 2). In
145 order to eliminate non-viable spatial models of neural coding from our analysis (see
146 below), we needed to record head-unrestrained gaze shifts in three dimensions (3-D).
147 To do this, two 5-mm-diameter sclera search coils were implanted in one eye of each
148 animal and two orthogonal coils mounted on the head (Crawford et al., 1999).

149 *Behavioral paradigm*

150 Monkeys were trained to perform the classic memory-guided gaze task in completely
151 head-unrestrained conditions (Fig. 1A). After fixating a visual stimulus presented on the
152 screen, a second visual stimulus (target) briefly flashed for 80-100ms in the periphery
153 cuing the gaze shift goal. However, the animal had to withhold gaze until the instruction
154 to make gaze shift (Go-signal = disappearance of fixation target) was provided, at which
155 time a gaze shift was made to the remembered location of the target. The Go-signal
156 was presented at a random time within a flat distribution that ranged 450-850ms (for
157 56/74 neurons) or 700-1500ms (for 18/74 neurons). Animals were allowed a relatively
158 large reward window of 5-12° in radius (visual angles) around the target. If the animal

159 kept gaze stable in the reward window for at least 200ms after the gaze shift, a juice
160 reward was provided. Visual stimuli were laser-projected on a flat screen, positioned
161 80cm away from the subject.

162 Our large reward window allowed animals to produce natural (untrained) errors in final
163 gaze direction (Fig. 1B). The variable component of these errors was necessary to
164 dissociate the most important models (i.e., target and gaze models) described below.
165 To quantify these we first calculated systematic gaze errors by computing the
166 parameters of the function $[dG = a_1 dT + a_2]$, separately for vertical and horizontal
167 components, where dG was gaze displacement and dT was target displacement from
168 initial gaze position. This revealed hypometria and vertical/horizontal offsets consistent
169 with previous studies of memory-guided saccades (De Bie et al., 1987; White et al.,
170 1994). Variable errors were quantified as the remaining errors that were unexplained by
171 the systematic errors (i.e., residuals of the linear fit). Variable errors in behavior were
172 distributed normally with SD in x-direction (SD_x)= 6.2, and in y-direction (SD_y) = 5.8 for
173 animal S, and $SD_x = 5.9$ and $SD_y = 5.7$ for animal A. The average magnitude of the
174 variable errors (mean \pm SD) was 6.3 ± 6 degrees. As we shall see, these values were
175 sufficient to statistically separate our target and gaze models, as were other variations
176 in 3-D eye and head orientation for the other models tested (Sajad et al., 2015).

177 *Extracellular Recording Procedures*

178 Extracellular activity from single FEF neurons was recorded using tungsten
179 microelectrodes (0.2-2.0 M Ω impedance, FHC). The neural signal was amplified,
180 filtered, and stored with the Plexon MAP system for offline cluster separation using
181 principal component analysis with the Plexon Offline sorter software. The recorded sites

182 were considered to be within the FEF if microstimulation with a current $<50 \mu\text{A}$ (70ms
183 trains of monophasic pulses; $300\mu\text{s/pulse}$, generated with a frequency of 300Hz)
184 evoked a saccade while the head was restrained (Fig. 2B; Monteon et al., 2010; 2012;
185 2013)

186 The search for neuron was conducted when the animal was freely scanning the
187 environment in a lighted room with the head free to move. When a neuron with clear
188 and stable spiking was isolated, the experiment began. A rough estimate of the
189 neuron's RF was first obtained using memory-guided gaze shifts to a wide spread of
190 targets presented one at a time from a central fixation point. Then an array of gaze
191 targets were set to cover the neuron's RF including the flanks of the RF (Fig. 1B, gray
192 dots). Targets were positioned in a rectangular array (ranging between 4×4 to 8×8 , 5-
193 10° apart depending on the size and shape of the RF). Initial fixation positions were
194 randomized within a central window with width ranging from 10 - 40° in proportion with
195 the estimated size of the RF (example shown in Fig. 1B).

196 *Data inclusion criteria (neurons and behavior)*

197 We recorded neuronal activity from over 200 sites in the FEF of the two animals.
198 However, since our method relies on detailed analysis of the RF of single neurons only
199 data from sessions for which we had clear isolation of spiking data were included to
200 eliminate any multi-unit activity from analysis. Also, only neurons for which enough trials
201 were recorded to uniformly cover a decent extent of the RF, and showed either visual or
202 pre-saccadic movement response types (or both) were included in the analysis. After
203 applying our exclusion criteria a total of 77 neurons were used for analysis (57 were

204 previously analyzed in another study). 3/77 neurons despite having clear visual and / or
205 movement response did not exhibit any spatial tuning and thus were eliminated. So, a
206 total of 74 neurons contributed to the results in this study. The anatomic distribution of
207 these neurons in the recording chambers is shown in Fig. 2B.

208 To obtain the behavioral data, the onset of gaze shift was defined as the time when the
209 gaze (eye in space) velocity exceeded $50^\circ/\text{s}$ and the gaze end-time was marked at the
210 time when velocity declined below $30^\circ/\text{s}$. Final gaze positions used for spatial analysis
211 were sampled at the gaze end-time. Individual trials were excluded offline if gaze shift
212 was clearly not directed towards the target, or the gaze error exceeded the regression
213 line of gaze error versus retinal error by at least two standard deviations (SD) (errors in
214 gaze end-point scale with gaze shift size). Furthermore, trials in which the subject made
215 an anticipatory gaze shift (with reaction time $< 100\text{ms}$ after Go-signal) were eliminated
216 to ensure that animals waited for the go-signal (extinction of the first fixation light) to
217 generate a saccade. In a behavioral analysis based on the same task in the same two
218 monkeys, it was confirmed that saccade onset correlated with the Go-signal (Sadeh et
219 al., 2015). Finally, trials in which the gaze, eye, and head were not stable during the
220 delay period were eliminated (for details see Sajad et al., 2015). After all trial exclusions
221 were applied, on average, 211 trials per neuron were used for analysis.

222 *Neuron classification*

223 We categorized neurons based on the temporal profile of their response (firing rate)
224 during visual, memory, and movement periods. Note that in this experiment each trial
225 was unique both in terms of the starting position and the metrics of the gaze shift and a

226 large proportion of trials were spatially spread outside of the RF hot-spot, the region
227 where the neuron is most responsive to. Therefore, in order to provide a measure of a
228 neuron's responsiveness we analyzed the activity of the neuron in the 10% of trials in
229 which the neuron was most active (Spk10) which would roughly correspond to trials that
230 fall near the center of the best-fit RF (see next section). Spk10 was calculated for
231 different time periods and used to identify whether a neuron had visual, delay, or
232 movement response as described below.

233 If Spk10 at 80-180ms after target onset (an early visual period) and/or -50 to +50ms
234 relative to gaze onset (peri-saccadic period) was higher than 25 spikes per second
235 (spk/s) relative to the pre-target baseline we characterized the neuron as having visual
236 and/or movement response (Sajad et al., 2015). A neuron was deemed responsive
237 during delay period if the average of the Spk10 during the 100ms period prior to the
238 presentation of the Go-signal was greater than 15spk/s and was significantly higher
239 than the trial-matched baseline (pre-target) activity levels ($p < 0.05$, Paired-sample
240 Wilcoxon Signed-rank Test). These criteria resulted in a classification similar to that
241 obtained by visual inspection: four classes including 1) visual (V) neurons which did not
242 exhibit movement activity, 2) visuomovement (VM) neurons which exhibited both visual
243 and movement responses, 3) delay-movement (DM) neurons which did not exhibit
244 visual response but showed delay activity prior to the Go-signal, and 4) movement-only
245 (M) neurons which only exhibited a movement response starting after the Go-signal.

246 *Model Fitting Procedures*

247 In order to systematically test between different spatial parameters, we fit spatial models
248 to RF data for every neuron using a procedure that has now been described several
249 times (Keith et al., 2009, DeSouza et al., 2011, Sajad et al., 2015, Sadeh et al., 2015).

250 In brief, the RF of the neuron was plotted by overlaying firing rate data (number of
251 spikes divided by sampling window width for each trial) over two-dimensional position
252 data corresponding to the spatial parameter related to the candidate model, such as
253 target position relative to the eye. The predictability power of the model for the recorded
254 data was quantified by obtaining Predicted Sum of Squares (PRESS) residuals across
255 all trials, which is a form of cross validation used in regression analysis (Keith et al.,
256 2009). Specifically, the PRESS residual for a single trial was obtained by: 1) eliminating
257 that trial from RF data, 2) fitting the remaining data points non-parametrically using
258 Gaussian kernels at various bandwidths (2-15°), and 3) obtaining the residual between
259 the fit and the missing data point. The overall predictability power of the model for the
260 recorded data set was quantified by the average of PRESS residuals across all trials for
261 that neuron. Examples of this process will be described below. Once PRESS residuals
262 of all tested models were obtained the spatial code was defined as the model (using the
263 kernel bandwidth) that yielded the overall best fit to the data.

264 In a preliminary analysis similar to that of our previous study (Sajad et al., 2015; which
265 used an overlapping but smaller population of neurons) we tested all of the models that
266 have been proposed for egocentric coding in the gaze control system against the visual
267 and movement responses of our neurons (we did not provide allocentric visual cues so
268 such models were not tested). This included models of target location vs. gaze, eye-in-
269 head, and head motion (both final position and displacement) in eye-centered, head-

270 centered, and body-centered frames of reference, for a total of 11 models (as noted
271 above, most of these tests required the use of 3-D head-unrestrained recordings). Since
272 this replicated our previous analysis on a smaller dataset, but with slightly better
273 statistics, we only summarize the results here.

274 Target location relative to initial eye orientation (T_e) was the best model for describing
275 our total population of visual responses, with all other models statistically eliminated
276 (Brown-Forsythe test). Future gaze position relative to initial eye orientation (G_e) gave
277 the best overall fit for our total population of motor responses, with all other models
278 statistically eliminated except for eye-in-head displacement and gaze displacement,
279 which were mathematically very similar to G_e . Therefore, we used T_e and G_e as the
280 best representatives of visual and motor coding, abbreviated henceforth as simple T
281 and G . Note that G is the visual axis in space controlled by both eye and head motion;
282 this is still head-unrestrained data.

283 Note that all of these models are correlated with each other to some extent (for
284 example, when the target is on the right, generally gaze, eye, and head move to the
285 right). This is why it has been so difficult to separate them using standard correlation
286 techniques (reviewed in Sajad et al. 2015). An advantage of our method is that it allows
287 each model fit to explain all of the variations in the data that it can (even if these arise
288 from cross-correlation), so that one then statistically compares only the data that the
289 model cannot explain (i.e., the residuals at each point on the RF). For example, to say
290 that G is statistically superior to T means that including errors in gaze position explains
291 variations that cannot be accounted for by T , and a superior fit for T means that G errors

292 introduce spatial variability in the fit that is not accounted for in the neural response.

293 However, it is also possible that the ideal fit comes somewhere between T and G .

294 *The Target-Gaze Continuum*

295 Unlike previous studies, which only made a distinction between T and G as two possible

296 spatial codes, we also considered intermediary codes between T and G by creating a

297 quantitative T - G continuum between and beyond these spatial models (Fig. 1D). This is

298 similar to the notion of intermediate reference frames (Bremner and Andersen, 2014;

299 Blohm et al., 2009; Avillac et al., 2005), but here we are taking intermediate codes for

300 two different variables within the same reference frame (eye coordinates). As described

301 in Sajad et al., (2015) these intermediate spatial models were constructed by dividing

302 the distance between target position and final gaze position for each trial into 10 equal

303 intervals and 10 additional intervals extended on either tail (beyond T and G). Figure

304 3A shows an example analysis of a visual response sampled from 80 to 180ms after

305 target onset. The RF plots corresponding to three spatial models along the T - G

306 continuum are shown in Figure 3A-2. In the RF plots, each circle represents firing rate

307 data (diameter) for a single trial plotted over position data corresponding to the tested

308 model (The circles are not shown in other RF plots throughout the paper). The color

309 code represents the non-parametric fit made to all data points (at a kernel bandwidth of

310 4 degrees, which was the bandwidth that yielded the overall best-fit for this neuron).

311 Below each RF plot, the PRESS residuals for all data points are shown, which provide a

312 measure for the predictability power of the model for the data points. The mean of the

313 PRESS residuals (mean PRESS) provided the overall predictability power of the model

314 for our dataset. 3A-3 shows mean PRESS (y-axis) as a function of tested spatial model

315 along the T - G continuum (x-axis). The model which provides the lowest mean PRESS
316 (marked by red arrow) is the model with the highest predictability power and thus is
317 identified as the spatial code of the neuron. For this example visual response the best-fit
318 model (i.e., spatial code) is the intermediate model one step away from T (towards G).
319 Note that the RF corresponding to the best-fit model (B, left panel) shows a relatively
320 high degree of *spatial coherence* with high neuronal response spatially confined to a
321 restricted region (red color). The most spatially-coherent fit would be a fit that gives the
322 lowest overall variance in the data relative to each point on the RF, corresponding
323 quantitatively to the lowest residuals of the fit. As the RF representation gets further
324 from the best-fit representation (middle, and right panels) the RF becomes progressively
325 less coherent (as visualized by size-gradient of the circles and the color map), and the
326 magnitude of the PRESS residuals increases.

327 *Time-normalization and activity sampling for spatiotemporal analysis*

328 The specific aims of this study required a new means of analyzing data that we have not
329 described previously: applying our spatial analysis through discrete time-steps spanning
330 the visual, delay, and motor responses of each trial. This proved challenging because
331 we used a variable delay period. In such a paradigm, aligning trials the standard way
332 (with either the visual stimulus or saccade onset) results in the loss and/or mixing of
333 activities across trials, and thus would not allow us to trace spatial coding through the
334 entire trial across all trials (Fig. 3B). To overcome this challenge, we normalized the
335 time between an early visual period and movement onset for all trials and applied our
336 analysis method to RFs sampled from the time-normalized activity profile. Our analytic
337 method thus treats time and space similarly, since the spatial codes tested in this study

338 (i.e., the *T-G* continuum) are also obtained through normalization of errors in behavior
339 (i.e., the vector difference between target position and final gaze position).

340 In order to sample neuronal activity using the time-normalized scheme, activity was
341 sampled starting from an early visual period, which was the onset of the visual activity
342 (mean = 87ms after target onset) for visually-responsive (V and VM) neurons and 80ms
343 after target onset for neurons with no visual response. The duration between this early
344 visual period and gaze movement onset was on average 895ms (\pm 234ms, SD) across
345 all trials. For spatiotemporal analysis the firing rate of the neurons (spikes/sec; number
346 of spikes divided by the sampling interval for each trial) was sampled at 16 half-
347 overlapping windows from this time-normalized data. This choice of sampling window
348 numbers was based on the approximate ratio of the duration of the visual response to
349 delay period to movement response including a post-saccadic period starting from gaze
350 onset (visual:delay:movement is approximately 3:10:3). The final (16th) time-step
351 corresponded to an entirely post-saccadic period starting from the onset of gaze shift.
352 Because of the time-normalization process the sampling window width scaled with the
353 duration between visual response onset and movement onset on a trial-by-trial basis.
354 On the 16-step time-normalized scale, the visual burst on average lasted 2.5 steps (SD
355 = 0.81 steps), ending by the end of the third time-step in 94.5% of trials. The
356 presaccadic duration was on average 1.35 steps (SD = 0.67), and for about 90% of the
357 trials started after the beginning of the 14th time-step. Therefore, in the time period
358 interleaving the first three and final three time-steps the sampled activity was largely
359 dominated by delay activity. The sampling window width was on average 119ms

360 (± 37 ms, SD) and was no less than 50ms for any trial which ensured enough neuronal
361 spikes captured in the sampling window to perform effective spatial analysis.

362 Thus, this time-normalization procedure allowed us to consider the entire sequence of
363 visual-memory-motor responses as a continuum. It causes blurring of some other
364 events across trials (e.g., the Go-signal), or mixing of visual and movement responses
365 in the delay period but these possibilities are controlled for in the Results section (see
366 Figure 8).

367 *Testing for spatial selectivity (for single neuron, and population)*

368 Our model-fitting approach would provide us with valid results if the sampled neuronal
369 activity exhibits spatial selectivity. Therefore, we excluded data points both at single
370 neuron level and at population level which did not exhibit significant spatial tuning of any
371 kind.

372 To test for spatial selectivity for a sampled response for an individual neuron we
373 compared the spatial selectivity of the best-fit representation with its random
374 counterpart. To do this, we randomly shuffled the firing rate data (number of spikes
375 divided by duration of the sampling window) and plotted them over the position data
376 corresponding to the best-fit model, and repeated this procedure 100 times to obtain
377 100 *random* RFs. The PRESS residuals of these random RFs (and their respective
378 mean PRESS values) were then obtained after fitting the data (non-parametrically,
379 using Gaussian kernels) with the same kernel bandwidth that was used to fit the best-fit
380 model, resulting in a total of 100 mean PRESS residuals. If the mean PRESS residuals
381 for the best-fit model ($\text{PRESS}_{\text{best-fit}}$) was at least 2SD smaller than the mean of the

382 distribution of random mean PRESS residuals (which was normally distributed), then
383 the sampled activity was identified as spatially-selective.

384 At the population level, even though at a given time-step some neurons exhibited spatial
385 tuning, due to low signal-to-noise ratio or few number of neurons contributing to the
386 population, our estimate for the population code would not be reliable. Therefore, we
387 excluded population data corresponding to time-steps at which the mean spatial
388 coherence of the population was not statistically higher from that of the pre-target
389 baseline which presumably exhibits no spatial tuning (as no task-relevant information is
390 available). The spatial coherence for each neuron contributing to the population spatial
391 coherence was measured using an index:

$$392 \text{ Coherence index} = 1 - (\text{PRESS}_{\text{best-fit}} / \text{PRESS}_{\text{random}})$$

393 Where $\text{PRESS}_{\text{random}}$ provided a measure of the predictability power for the random
394 distribution (average of mean PRESS residuals over the 100 independent distributions).
395 If $\text{PRESS}_{\text{best-fit}}$ was approximately similar to $\text{PRESS}_{\text{random}}$ then coherence index would
396 be a value around 0. Alternatively, if $\text{PRESS}_{\text{best-fit}} = 0$ (which would only occur when the
397 model perfectly accounted for the data) the index would be 1. The coherence index can
398 also be used to determine the amount of variance in the neural data described by the
399 best-fit model. In our data the range of coherence indices was from -0.07 to +0.67. We
400 did not expect coherence index to be 1 especially because neurons in the FEF are
401 shown to be modulated by other non-spatial factors such as attention and reward
402 expectancy (Schall, 2015).

403 *Non-parametric fits to temporal progress of spatial code in single-neurons*

404 The spatiotemporal progression of the neuronal code was analyzed by plotting the best-
405 fit model (y-axis) as a function of the discretely sampled time-steps (x-axis). To visualize
406 these trends (and for the population analysis in the next section) we performed a non-
407 parametric fit to this data for each neuron. Only data corresponding to spatially-tuned
408 time-steps contributed to the fit. Fit values were included for every time-step whose two
409 neighboring time-steps (both before and after) exhibited spatial tuning. The fit was
410 discontinued for the range at which at least two consecutive time-steps were not
411 spatially-tuned. Gaussian kernel with bandwidth of 1 time-step was used for non-
412 parametric fitting of this data. This choice was made conservatively to avoid over-
413 smoothing the data. As can be noted in Figures 5,6,8,9,10, the fit values closely
414 matched the data points obtained for individual neurons. Unless stated otherwise, we
415 used the fit values, rather than individual data points, for statistical tests reported in this
416 study, because they were less likely to be influenced by outliers.

417 *Population analysis and comparison between neuronal sub-populations*

418 Since most theoretical papers suggest that it is neural populations, not individual
419 neurons, that matter most for behavior (Pouget and Snyder, 2000; Blohm et al., 2009),
420 the results presented here focus mainly on our *T-G* analysis of our entire population of
421 neurons as well as several sub-populations (V, VM, DM, M). The overall population
422 coding preference across the *T-G* continuum (continuous trend-lines in Figures 4E, 5B,
423 6B, 7, 8B, 9B) at any given time-step was defined as the mean of the fits made to
424 individual neuron data. Since the distribution of spatial code within different neuronal
425 sub-populations did not exhibit a normal distribution, we used non-parametric statistical
426 tests to compare between data across the population, as well as the regression

427 analyses presented in the Results for VM and DM neurons.

428 **Results**

429 We recorded neurons from over 200 sites in the FEF during head-unrestrained
430 conditions. After applying our rigorous data exclusion criteria, 74 neurons were included
431 in the analysis (see Materials and Methods; Fig. 2). This is a very large number of
432 neurons compared to other head-unrestrained studies (e.g., Freedman and Sparks
433 1997; Knight, 2012). However, it is not large compared to some head-restrained
434 studies, so we limited our analysis to data that showed significant spatial tuning, and
435 limit our conclusions to the statistically significant neural population results described
436 below.

437 As described in the Materials and Methods, our preliminary data analysis corroborated
438 the findings of the previous study (Sajad et al., 2015), i.e. that target-relative to initial
439 eye orientation (T) provided a significantly preferred fit for the full population visual
440 response and future gaze position relative to initial eye orientation (G) provided the best
441 overall fit for the full population motor response. We henceforth focus on the temporal
442 transition along the T - G spatial continuum between these two events.

443 Figure 4A shows the activity profile of a typical neuron with visual, sustained delay, and
444 movement responses using the standard conventions of aligning activity with either the
445 onset of the visual stimulus (left panel) or the onset of the gaze shift (right panel). Figure
446 4B shows the time-normalized spike density plot corresponding to the raster and spike
447 density plots in Figure 4A. The RF maps obtained at four representative time-steps (C1-
448 C4) from these data are also shown. This neuron had a very sharp (small) and spatially-
449 distinct (bound) visual RF (C1), and a similar movement RF (C4). The delay-related

450 activity (C2, C3) exhibited similar spatial tuning, but the RF was more constricted and
451 less spatially organized. After applying our *T-G* continuum analysis we observed a
452 progressive shift of the best-fit model from *T* part-way toward *G* (shown by red icons
453 above the RF plots in Fig. 4C) as activity progressed in time. This trend was often
454 observed in our preliminary analysis and thus prompted the population analyses that
455 follow.

456 **Mixed Population Analysis**

457 Figure 4D shows the mean, time-normalized spike density profiles of the 74 neurons
458 that qualified for our analysis (see Materials and Methods). This reveals the typical
459 visual response (present in 52/74 neurons), followed by activity that was statistically
460 significant during some or all of the delay period (present in 51/74 neurons), and the
461 typical movement response (present in 64/74 neurons) of the FEF. For our model-fitting
462 procedure, we sampled this data through 16 half-overlapping time-steps (see Materials
463 and Methods). The activity at each time-step was first tested for spatial tuning and then
464 the spatial code (i.e., best-fit model) was included if the test was positive. At least 50%
465 of neurons were spatially selective at each time-step (see histograms in Fig. 4E, bottom
466 panel).

467 The mean of the individual data points at each time-step ($\circ \pm \text{SEM}$) as well as the fits
468 made to each neuron's data points (black line) for spatially-selective responses at every
469 time-step is shown in Figure 4E (The median was nearly identical in this dataset, not
470 shown). Importantly, this method of illustrating the data (which we will use henceforth)
471 provides the full spatiotemporal continuum of information coded by the population, by

472 showing best-fits along the *T-G* continuum as a function of our 16 time-steps through
473 the normalized evolution of the trials. These data reveal that the overall population best-
474 fit model started from a location near *T* and monotonically and almost linearly moved
475 towards *G* as activity evolved from dominantly vision related – through the delay activity
476 – to movement related ($R_s = 0.90$, $p = 2.44 \times 10^{-6}$, Spearman's ρ correlation). On
477 average, for the spatially-tuned responses the best-fit intermediate *T-G* model explained
478 21% of the variance in the early visual activity (1st time-step), while it decreased to
479 approximately 12-13% during mid-delay (7-9th time-steps), and 23 % in the peri-
480 saccadic movement period (15th time-step). Since these results were better than any of
481 the other comprehensive list of spatial models we tested, this unaccounted variance
482 was presumably due to non-spatial factors such as attention, motivation, and random
483 noise.

484 The *T-to-G* progression is not due to temporal smoothing of responses between the
485 visual-memory transition and memory-motor transition (Figure 3B), because similar
486 trends and statistics were observed when the visual and motor responses were
487 removed entirely from the analysis (this is illustrated for VM neurons with sustained
488 delay activity in Fig. 8). Framed in terms of our model-fitting method, these results mean
489 that the population activity is initially unrelated to future gaze position errors, but as the
490 memory interval progresses, these variable gaze errors are increasingly reflected within
491 the population code. Separate analysis of shorter vs. longer memory intervals (not
492 shown) yielded no difference in the results.

493 To examine the contribution of different cell types to this progression in spatial coding,
494 we subdivided our population into four subpopulations, based on whether or not they

495 had visually-evoked, delay-, or movement-related activities (see below, and Materials
496 and Methods) and performed the same analysis for each sub-population (Bruce and
497 Goldberg, 1985).

498 **Neurons with Visual Responses (Visual and Visuomovement Neurons)**

499 Our population of neurons with visual responses was further divided into two classes
500 based on whether or not they also exhibited movement activity (see Materials and
501 Methods for quantitative definitions of each neuron class). In total, we had 10 V
502 neurons and 42 VM neurons. For these neurons, activity was sampled through time
503 from visual response onset until a post-saccadic period starting at the onset of the gaze
504 movement, using only the epochs that tested positive for spatial tuning.

505 *Visual neurons*

506 Figure 5A shows the spike density profile (top panel) and model fits through time
507 (bottom panel) for a typical V neuron, with a strong visual response but little or no delay
508 or movement-related activity showing typical results. This neuron only exhibited spatial
509 tuning (see Materials and Methods) at the first four time-steps. The RF plot (in the best-
510 fit representation) corresponding to the first time-step, which corresponds to the early
511 visual activity is shown in Figure 5A (bottom panel) showing that this visual neuron had
512 a small and bounded RF with sharp spatial tuning. At all four time-steps the T - G
513 continuum analysis provided fits near the T model (Fig. 5A, bottom panel). Most visual
514 neurons showed a similar trend for T preference in the visual response, consistent with
515 our previous results (Sajad et al., 2015). Figure 5B illustrates the corresponding
516 analysis for the entire V neuron population, showing the mean spike density profile

517 (upper panel) and model fits through time using conventions similar to Figure 4D and
518 4E. Across the V population only the first three time-steps (corresponding to the visual
519 transient response) exhibited significantly higher spatial coherence (lower fit residuals)
520 than the pre-target period ($p < 0.05$; green colored data). Of the fits at these time-steps
521 (green circles), the first were very near to T . The next two time-steps showed a trend to
522 drift toward G , but none were significantly different from T ($p > 0.05$, One-
523 sample Wilcoxon Signed-Rank Test). Although some V neurons showed declining
524 activity during the delay period, this did not pass our population spatial tuning criteria
525 (see Materials and Methods), and gave highly variable fits (gray shaded area) that were
526 not further considered.

527 *Visuomovement neurons*

528 A similar analysis was performed on VM neurons. VM neurons were particularly of
529 interest in this study because they exhibited both a visual and a movement response,
530 and unlike V neurons, a large proportion of them exhibited delay activity ($n = 36/42$).
531 Figure 6A (top panel) shows the time-normalized spike density plot for an example VM
532 neuron with a large visual response followed by a delay response leading to a small
533 movement response. This neuron exhibited significant spatial tuning at all 16 time-
534 steps. The early visual response of this example was best described by intermediary
535 models almost at the mid-point between T and G . However, from the third time-step
536 onward, there was a monotonic change in the best-fit model from a model near T to a
537 model near G (Fig. 6A, bottom panel). RF plots corresponding to the highlighted time-
538 steps in panel A (bottom panel) are shown in panel C. Similar to the VM example shown
539 in Figure 4A-C, although the RFs corresponding to the delay period is attenuated and

540 more spatially restricted compared to the visual and movement RFs, they cover the
541 same relative spatial position, though the spatial model that best fits each is different.
542 The change in spatial code from T to G was present in the majority of VM neurons with
543 delay activity: of the neurons that showed delay activity, 29/36 showed a positive
544 increment along the T - G continuum. However, the degree of this change was variable
545 across neurons (mean $+4.65 \pm 6.47$ Standard deviation in T - G units).

546 The monotonic (constant direction) change in spatial code from T to G was also
547 observed at the population level in the VM neurons ($n = 42$) (Fig. 6B). Specifically, the
548 mean population code in the first time-step (corresponding to early visual response) fell
549 close to T (two steps towards G along the T - G continuum), but unlike V neurons it was
550 significantly different from T ($p = 3.2 \times 10^{-5}$, One-sample Wilcoxon Signed-Rank Test).
551 The mean population code then progressed monotonically (almost linearly) towards G
552 ($R_s = 0.91$, $p = 9.08 \times 10^{-7}$, Spearman's ρ correlation). However, at the final time-step
553 (corresponding to a period within the movement response and just after gaze onset), it
554 was still significantly different from G ($p = 3.51 \times 10^{-7}$, One-sample Wilcoxon Signed-
555 Rank Test; Fig. 6B, bottom panel).

556 Figure 7A illustrates how the distribution of best-fits for VM neurons evolves through
557 time. Specifically, this histogram plots the best fit T - G distributions for the early-visual
558 (step 1), early-delay (step 4), mid-delay (step 9), late-delay (step 13), and
559 perimovement (step 15) intervals. Focusing on the delay activity (middle three panels),
560 this population did not show a bimodal distribution of T - G with a diminishing T peak
561 while G codes rose. Instead, during the delay, spatially tuned VM neurons showed a
562 broad distribution of T - G codes that progressive shifted toward G (this shift is most

563 easily observed in the population means and medians, illustrated as vertical black and
564 green lines).

565 To visualize how this occurs at the level of individual neurons, we plotted the delay T - G
566 fits as a function of the motor T - G fits for each VM neuron that showed significant
567 spatial tuning at all 5 time-steps ($n=21$). The top panel, corresponding to early-delay
568 epoch, shows that the majority of the data points were shifted below the line of unity,
569 toward the T -end of the distribution. Indeed, at this point in time the distribution is not
570 significantly different from the visual distribution (0.3052, Paired-sample Wilcoxon
571 Signed Rank Test). However, as the activity progresses through the mid- (middle panel)
572 and late-delay (bottom panel) intervals the data points progressively migrate upwards,
573 finally clustering more tightly around the motor code. At the late-delay interval, this
574 difference is significantly different from the visual fits for the same population of neurons
575 ($p = 0.0190$, Paired-sample Wilcoxon Signed Rank Test). When we further reduced this
576 population to only those cells that showed significant spatial tuning at every single time-
577 step of the delay ($n=16$), 13 of these neurons showed a positive slope in the T -to- G
578 direction during the delay period (mean slope = 0.36 T - G units per time-step, $SD = 0.52$
579 T - G units per time-step).

580 Collectively the results reported above support the notion that in the VM population (and
581 most individual VM neurons) the spatial code is not stable during the delay period but
582 rather changes through the intermediate range between T and G , starting at a point
583 closer to a target code and ending at a point closer to a gaze code.

584 To ensure that the *T-G* transition described above was not influenced by our time-
585 normalization procedure, or temporal blurring of spatial responses across different
586 epochs, we performed a more detailed technical analysis. For this technical analysis,
587 we used the best possible data we could obtain from our full dataset. First, we removed
588 any VM neurons that showed any temporal discontinuity during the delay, i.e., leaving
589 only those that showed sustained activity throughout the entire delay period ($n = 22$).
590 Then, we repeated our time-normalized analysis (Fig. 8A) on these data. This yielded
591 very similar trends and statistics to that observed for the overall population (linear
592 progressive trend in change from a code near *T* to a code near *G*; $R_s = 0.86$, $p = 2.40 \times$
593 10^{-5} , Spearman's ρ correlation).

594 Next, we performed a similar time-normalized analysis, but excluded the visual and
595 movement responses for every neuron (Fig. 8B). Once again a monotonic change in
596 spatial code with a significant slope ($R_s = 0.76$, $p = 0.0038$, Spearman's ρ correlation)
597 was observed. These results show that the progressive change in the spatial code
598 described above (Fig. 4, 6, 8A) is *not* due to the temporal smoothing of delay codes
599 with visual and movement responses.

600 Finally, we controlled for the possibility that the *T-G* transition might have been caused
601 by specific events within each trial, and that our time normalization technique might
602 have blurred these events through time to create an apparently progressive *T-G*
603 transition (see Materials and Methods, and Fig. 3B). Specifically, activity was aligned
604 with three major task events (Fig. 8C), namely, target onset (left panel), Go-signal
605 (middle panel), and movement onset (right panel). The target-aligned analysis (left
606 panel) was performed from 80ms after target onset until the earliest Go-signal. In this

607 period, (which was roughly equivalent for all trials for a given neuron irrespective of
608 delay duration) the change in spatial code did not greatly contribute to the overall
609 change in spatial code (Fig 8C, left panel). Notably, the spatial code (both mean of the
610 individual data points and the mean of the fits) was stable both before and after Go-
611 signal (Fig 8C, middle panel), suggesting that the change in spatial code was not
612 prompted by this signal. The same observation held for gaze movement onset (Fig 8C,
613 right panel). Collectively, these control results reinforce our main result; that the spatial
614 code during memory period changes progressively across the entire delay interval,
615 rather than discretely under the influence of specific task events.

616 **Neurons with no visual response (Delay-Movement and Movement-only Neurons)**

617 In our population, 22 neurons exhibited movement response but lacked visual response.
618 This movement population was further classified into two classes: Movement neurons
619 with activity starting at least 100ms before the appearance of the Go-signal were
620 classified as DM neurons ($n = 12$) and those with activity only appearing after the Go-
621 signal were classified as M neurons ($n = 10$) (see Materials and Methods). Since these
622 neuron types lacked a visual response, the first time-step used for our spatial fits (Fig. 9,
623 10) started from a fixed time (80ms) after target onset.

624 *Delay-Movement Neurons*

625 Figure 9A shows the time-normalized spike density plot for a representative DM neuron,
626 with activity beginning 150ms after target onset, sustaining through the delay period,
627 and leading into a pre-saccadic buildup towards the peak just around the time of gaze
628 onset. This neuron first showed a spatially-tuned response at the third time-step. The

629 RF plots corresponding to the 5th, 10th, and 15th (centered on gaze onset) time-steps
630 are shown in Figure 9C. Although there was a sudden rise in firing rate at around the
631 time of gaze shift, there was no major change in the spatial code of this neuron through
632 time. Instead, throughout the delay and motor epochs the spatial code of this neuron
633 remained intermediate between T and G . At the population level, spatial coherence of
634 DM neurons became significantly higher than the pre-target period at the 4th time-step
635 and thereafter. At all these time-steps the spatial code remained at an intermediate
636 position between T and G , and significantly different from both T ($p = 4.88 \times 10^{-4}$) and G
637 ($p = 0.0015$), even during the movement response, just after gaze onset (i.e., final time-
638 step) (One-sample Wilcoxon Signed-Rank Test). There was no apparent trend for
639 change in the DM fits during the delay period (Fig. 9B). Consistent with this, there was
640 no significant correlation between spatial code and time-step ($R_s = 0.47$, $p = 0.20$,
641 Spearman's ρ correlation).

642 *Movement-only neurons*

643 Figure 10A (top panel) shows the activity of an example M neuron with activity rising
644 just before the onset of the gaze shift (about 120ms before saccade onset). This neuron
645 only showed spatial tuning for four time-steps around the time of gaze onset, showing a
646 spatial code tightly centered around G (Fig. 10A, bottom panel). The RF plot shown
647 here corresponds to the time-step centered at gaze onset. For the M population only the
648 three time-steps straddling gaze onset showed significantly higher coherence index
649 than the pre-target period (with other time-steps shown in gray; Fig. 10B). In all the
650 time-steps in the motor epoch population spatial code was very close to G (less than

651 one step short of G along T - G continuum) and was not significantly different from G ($p >$
652 0.25 for each time-step, One-sample Wilcoxon Signed-Rank Test).

653 **Summary of results and comparison of sub-populations**

654 Figure 11A summarizes and compares the results for each of the neuron sub-
655 populations described above, by superimposing their population means and confidence
656 intervals within a single normalized spatiotemporal continuum plot. Based on the
657 amount and coherence of activity in the sub-population results described above, we
658 have divided the neuronal responses into a visual epoch (first three time-steps), the
659 delay epoch (next 10 time-steps), and the motor epoch (final three time-steps,
660 straddling gaze onset). During the visual epoch, V neurons start with a code very close
661 to T , but tend to converge toward the VM code (V and VM were not significantly
662 different in their three shared time-steps). Both the VM and DM populations showed an
663 intermediate spatial code throughout the delay period, as described above. There was
664 no statistical difference between these two populations at any shared time-steps ($p >$
665 0.20 , two-tailed Mann-Whitney U test) and the slopes of the regression lines to
666 individual data points (not shown) were not significantly different ($p = 0.87$, linear
667 regression comparison). However, as described above only VM neurons showed a
668 significant slope. The VM trend-line starts closer to T , crosses the DM line about
669 halfway through the delay epoch, and then ends up closer to (but still significantly
670 different from) G . In summary, only VM neurons showed a significantly positive T - G
671 slope, but all spatial coding along the T - G continuum during the visual and delay epochs
672 (in V , VM , and DM populations) was similar, and all three would have contributed to the
673 overall population code in these epochs.

674 The most striking difference between sub-populations occurs toward the end, during the
675 motor epoch. Although three sub-populations are active at this point, only one (M) is not
676 significantly different from G, and is significantly different from both the DM and VM
677 neuron fits ($p = 6.16 \times 10^{-5}$ and $p = 3.49 \times 10^{-5}$ respectively, Bonferroni-corrected two-
678 tailed Mann-Whitney *U* test; using data pooled across the three final time-steps roughly
679 corresponding to the motor epoch). We noted that VM neurons (but not DM neurons)
680 showed a noticeable peak in their *T-G* distribution falling between the *T-G* midpoint and
681 G (Figure 7a, bottom panel), and wondered if these neurons contributed more to the
682 motor output. However, when we repeated the preceding statistical comparison,
683 restricting the VM population to these more G-like codes ($n = 27$), the difference from M
684 neurons was still significant ($p = 0.0127$, two-tailed Mann-Whitney *U* test).

685 To summarize, the overall impression across all four populations is of a gradual shift in
686 coding from *T* (in the pure visual response) toward an intermediate *T-G* code (relayed
687 between the V, VM, and DM populations), with a final discrete shift in coding toward G
688 (i.e. a pure motor code) in the M population.

689 **Discussion**

690 This is the first study to describe the entire spatiotemporal sequence of visual-memory-
691 motor transformations during head-unrestrained gaze shifts toward remembered visual
692 stimuli. The current study was motivated by our previous study, which used a memory-
693 delay task to show that 1) FEF visual activity codes target position (*T*) whereas 2) peri-
694 saccadic motor activity codes future gaze position (*G*) (Sajad et al., 2015), but we did
695 not show *when* or *how* this transition occurred. Further, we did not show how different
696 cell populations contributed to this transition. Here, we addressed these questions by
697 using a larger dataset (30% more neurons) and a new analytic method to track spatial
698 coding along the *T-G* continuum through time. This resulted in two novel and important
699 findings: 1) FEF delay activity (particularly in VM cells) showed a *progressive* evolution
700 through intermediate *T-G* codes, and 2) an additional discrete jump occurred between
701 intermediate *T-G* coding in the late delay / motor activity of VM and DM cells, to *G*
702 coding in M-only cells during the final memory-motor transformation for saccades.

703 Our methodology combined several advantageous approaches: 1) head-unrestrained
704 recordings (necessary to eliminate non-relevant spatial models in our preliminary
705 analysis, and to provide the best behavioral estimate of frontal cortex output; Corneil et
706 al., 2007; Paré et al., 1994; Martinez-Trujillo et al., 2003; Sajad et al, 2015), 2) a simple
707 memory-delay saccade paradigm (avoiding the interpretive issues associated with
708 sensory-motor dissociation tasks; Johnston et al., 2009; Hawkins et al., 2013), and 3)
709 considering possibility for intermediate spatial codes rather than adhering to the
710 traditional binary classification of the spatial code as sensory or motor (the significance
711 of this will be further elaborated below). To our knowledge, this is the first time such a

712 combination of techniques has been applied to the FEF or any other brain area to
713 characterize the spatial codes in delay period. Although head-unrestrained recordings
714 were critical for narrowing down our analysis to T and G (and hence the intermediate T -
715 G) models, similar results would be expected in head-restrained conditions provided
716 that there is enough variability in behavior to adequately separate T and G .

717 **Intermediary codes in the delay period**

718 Several previous studies have proposed that spatial working memory evolves through
719 time from a sensory to motor code, when these are dissociated in some fashion
720 (Goldman-Rakic, 1987; Gnadt et al., 1991; Fuster, 2001; Postle, 2006). Consistent with
721 this, Takeda and Funahashi (2004) showed that the population spatial code in dlPFC
722 progressively rotates from a sensory vector to a motor vector during a memory delay, in
723 animals trained to rotate saccade direction relative to visual direction. Zhang and
724 Barash (2004) showed a reversal from 'pro' to 'anti' coding across LIP neurons in the
725 delay preceding anti-saccades. In the current study we found that FEF delay activity
726 showed a progressive transition from a T code that faithfully indicated target location,
727 through intermediate T - G codes that approached, but did not quite reach coding future
728 gaze position. This T - G progression was statistically significant at the neural population
729 level, and we observed similar trends in at least some neurons. This finding differs from
730 results of studies that spatially dissociated from the presented visual stimulus by virtue
731 of cognitive manipulations (such as rotation or reversal) of the sensory vector
732 (Funahashi, 1989, 1993; Takeda and Funahashi, 2002). In these studies, the
733 sensorimotor transition involved a progressive decrease of activity in visually-tuned cells
734 combined with a progressive increase of activity in motor-tuned cells (Takeda and

735 Funahashi, 2004, 2007; Zhang and Barash, 2004). We did not observe this in our
736 simpler memory-delay task, but rather a progressive change in coding along the *T-G*
737 continuum within the same population (i.e., VM neurons), even within neurons.

738 To our knowledge, only one other neurophysiological study has considered the change
739 in spatial code within one population of neurons during a memory delay. Wimmer et al.,
740 (2014) found that activity in the dIPFC showed increased correlations with variations in
741 final gaze position during a memory-delay period. Since the *T-G* transition observed in
742 our results signifies a progressively increased correlation of FEF delay activity with gaze
743 errors (discussed below), it resembles previous dIPFC results (Wimmer et al., 2014).
744 Similar results in FEF and dIPFC are in agreement with their reciprocal connectivity and
745 their close relationship in the maintenance of working memory (O'Sullivan et al., 1995;
746 Sweeney et al., 1996; Offen et al., 2010). Note that the main source of the *T-G*
747 progression within our full FEF population appeared to be VM neurons (Fig. 6-8). This
748 trend was statistically significant in VM neurons, whereas, DM neurons did not show a
749 statistically significant progression (Fig 9B). There is currently no clear consensus
750 whether both classes of neurons contribute to the psychological phenomenon of
751 working memory (Simon et al., 2002; Lawrence et al., 2005; Heinzle et al., 2007;
752 Sommer and Wurtz, 2001). However, a survey of previous publications suggests that
753 DM neurons might be more closely associated with motor planning, whereas VM
754 neurons may be more closely associated with mnemonic functions (Takeda and
755 Funahashi, 2007; Takaura et al., 2011; Markowitz et al., 2015). This notion is
756 consistent with findings that visually-responsive neurons are responsible for retaining
757 and updating visual memory in the superior colliculus (SC) (Sparks and Porter, 1983;

758 Dash et al., 2015). Alternatively, it may be that all delay-responsive neurons in the gaze
759 network are connected through an internal feedback loop for working memory, and
760 influence each other's spatiotemporal profiles (Verduzco-Flores et al., 2009; Okamoto et
761 al., 2007; Curtis 2006).

762 **Transformations between sensory, memory, and motor codes**

763 The second novel observation in this study was the demonstration of discrete changes
764 in the spatial code towards G, in the transition *between* visual, memory, and motor
765 signals. Some theoretical studies have considered spatial transformations throughout
766 this sequence of events (Brown et al., 2004; Faisal et al., 2008; Ma et al., 2014), and
767 some experimental oculomotor studies have inferred from their data that additional
768 memory-to-motor transformations must occur after the delay period (Stanford and
769 Sparks, 1994; Opris et al., 2003). However, to our knowledge, these transformations
770 have never been directly identified in neural signals. Here we have relied on the
771 presumption that transformations between functional networks are inherently noisy
772 (Alikhanian et al., 2015; Ma et al., 2014; Faisal et al., 2008) to infer the occurrence of
773 transformations based on discrete accumulations of variable errors. Our data suggest
774 that spatial transformations might occur upstream from VM neurons, because they
775 already show a slightly shifted intermediate code at the start of the visual response. As
776 described above, further transition of spatial code occurs during the memory delay,
777 possibly due to degrading memory representations, but importantly, there is an
778 additional transition from an intermediate *T-G* code in VM/DM neurons to a pure *G* code
779 in M neurons at the end of the delay period (even when only compared VM vs. M
780 neurons with preference for gaze-related models). To our knowledge, this is the first

781 direct demonstration of a memory-to-motor transformation between cells within the
782 same structure.

783 **Conceptual Model and Sources of Variable Error**

784 It is important to note that our model-fitting method relies on the relationship between
785 variability in neural firing rate and variability in behavior. In particular, the *T-G* continuum
786 reflects the degree to which neural firing rate faithfully represents target location for an
787 idealized saccade, versus the variable errors in actual future gaze direction. Thus, the
788 *T-G* scores shown in Figure 11A can be interpreted as reflecting the progression of
789 gaze error coding in different neural populations through time. With this in mind, Figure
790 11B schematically summarizes the possible flow of spatial signals within the FEF during
791 our task, and how these mechanisms might contribute to gaze variations.

792 According to this model, both V and VM neurons receive relatively unprocessed spatial
793 information about the location of the visual stimulus relative to the eye but VM neurons
794 receive additional inputs from V (and perhaps other areas) containing errors that tend to
795 shift the spatial code slightly further toward *G* along the *T-G* continuum. This spatial
796 information is then maintained within a working memory / planning network comprised
797 of VM and possibly DM neurons, as well as their extrinsic connections (Zelinsky and
798 Bisley, 2015). Here, the spatial representation in VM neurons shifts through
799 intermediary *T-G* codes throughout the delay period, presumably through the
800 accumulation of noise in a recurrent feedback network (Burak and Fiete, 2012; Compte
801 et al., 2000; Wang et al., 2015). Upon the presentation of the Go-signal, the retained
802 spatial information is then disinhibited, thus producing the motor response in VM and

803 DM neurons. At the same time, this code is relayed to the M neurons, involving an
804 additional transformation, pushing the final motor code almost to G. This is consistent
805 with the notion of noise arising in the transformation from memory to motor network
806 (Zheng and Wilson, 2002; Alikhanian et al., 2015; Avery and Krichmar, 2015). These
807 signals could then influence behavior through projections to the brainstem (Kunzle et
808 al., 1976; Segraves, 1992). For example, we have observed similar noisy gaze-related
809 signals in the motor responses of the SC (Sadeh et al., 2015).

810 Overall, these observations suggest that the noisy gaze signal that we observed in the
811 overall motor response in our previous study (Sajad et al. 2015) is not the result of a
812 random or general degradation of visual signals, but rather arises from different sources
813 and different types of cells that relay different signals through different synaptic
814 networks (Lawrence and Snyder, 2005; Chatham and Badre, 2015; Markowitz et al.,
815 2015). To simple terms, our data support a combination of the gradual progression
816 model and late transformation models illustrated in Figure 1D.

817 **Behavioral and Clinical Implications**

818 The noise-source model shown in Figure 11B could be useful for understanding and
819 investigating behavior in both healthy and clinical populations. It is reasonable to
820 assume that the sources of these variable errors would be vulnerable to diseases that
821 affect frontal cortex function (Avery and Krichmar, 2015). If so, this confirms that
822 analysis of variable errors in memory-delay saccade task has diagnostic value for
823 diseases that affect frontal cortex function (Ploner et al., 1999). Further, whereas most
824 behavioral studies interpret errors from memory delay tasks only in terms of

825 maintenance (e.g., Oyachi and Ohtsuka, 1995; D'Esposito and Postle, 1999; Wimmer et
826 al., 2014) or transformations (e.g., Henriques et al., 1998; Vesia et al., 2010; Dessing et
827 al., 2012), our study confirms that both maintenance and memory-to-motor
828 transformations must be taken into account (Gnadt et al., 1991; Avery and Krichmar,
829 2015). For example, numerous clinical studies have considered errors that arise in
830 working memory maintenance (Minshew et al., 1999; Sweeney et al., 2007; Mazhari et
831 al., 2010), but there is also evidence that errors arise in the gating of memory signals to
832 action in Parkinson's and Schizophrenic patients (Avery and Krichmar, 2015; Ketcham
833 and Stelmach, 2003; Rottschy et al., 2013). Thus, the observed errors in these patients
834 could be interpreted as degraded states of noisy memory and memory-to-motor
835 transformations observed here.

836 **References**

- 837 Alikhanian H, de Carvalho SR, Blohm G (2015) Quantifying effects of stochasticity in
838 reference frame transformations on posterior distributions. *Front Comput Neurosci*
839 9:82. doi: 10.3389/fncom.2015.00082.
- 840 Avery MC, Krichmar JL (2015) Improper activation of D1 and D2 receptors leads to
841 excess noise in prefrontal cortex. *Front Comput Neurosci*.
842 Doi:10.3389/fncom.2015.00031
- 843 Avillac M, Deneve S, Olivier E, Pouget A, Duhamel JR (2005) Reference frames for
844 representing visual and tactile locations in parietal cortex. *Nat Neurosci* 8:941-949.
- 845 Bays PM, Gorgoraptis N, Wee N, Marshall L, Husain M (2011) Temporal dynamics
846 of encoding, storage, and reallocation of visual working memory. *J Vis* 11(10) doi:
847 10.1167/11.10.6.
- 848 Blohm G, Keith GP, Crawford JD (2009) Decoding the cortical transformations for
849 visually guided reaching in 3D space. *Cereb Cortex* 19(6):1372-1393
- 850 Bremner LR, Andersen RA (2014) Temporal analysis of reference frames in parietal
851 cortex area 5d during reach planning. *J Neurosci* 34:5273-5284.
- 852 Brown JW, Bullock D, Grossberg S (2004) How laminar frontal cortex and basal
853 ganglia circuits interact to control planned and reactive saccades. *Neural Networks*
854 17:471-510.
- 855 Bruce CJ, Goldberg ME (1985) Primate frontal eye fields. I. Single neurons
856 discharging before saccades. *J Neurophysiol* 53:603-635.

- 857 Burak Y, Fiete IR (2012) Fundamental limits on persistent activity in networks of
858 noisy neurons. *Proc Natl Acad Sci U S A* 109:17645-17650.
- 859 Chatham CH, Badre D (2015) Multiple gates on working memory. *Curr Opin Behav*
860 *Sci* 1:23-31.
- 861 Compte A, Brunel N, Goldman-Rakic PS, Wang X-J (2000) Synaptic mechanisms
862 and network dynamics underlying spatial working memory in a cortical network
863 model. *Cereb Cortex* 10:910-923.
- 864 Constantinidis C, Franowicz MN, Goldman-Rakic PS (2001) The sensory nature of
865 mnemonic representation in the primate prefrontal cortex. *Nat Neurosci* 4:311-316.
- 866 Corneil BD, Munoz DP, Olivier E (2007). Priming of head premotor circuit during
867 oculomotor preparation. *J Neurophysiol* 97(1):701-714.
- 868 Crawford JD, Ceylan MZ, Klier EM, Guitton D (1999) Three-dimensional eye-head
869 coordination during gaze saccades in the primate. *J Neurophysiol* 81:1760-1782.
- 870 Curtis CE (2006) Prefrontal and parietal contributions to spatial working memory.
871 *Neuroscience* 139(1):173-180.
- 872 Curtis CE, D'Esposito M (2006) Selection and maintenance of saccade goals in the
873 human frontal eye fields. *J Neurophysiol* 95:3923-3927.
- 874 Dash S, Yan X, Wang H, Crawford JD (2015) Continuous updating of visuospatial
875 memory in superior colliculus during slow eye movements. *Curr Biol* 25:267-274.

- 876 De Bie J, Brink V, Van Sonderen J (1987) The systematic undershoot of saccades:
877 A localization or an oculomotor phenomenon? In: J.K. O'Regan and A. Levy-
878 Schoen, Editors, eye movements: From physiology to cognition, Elsevier, New York,
879 85/94.
- 880 DeSouza JFX, Keith GP, Yan X, Blohm G, Wang H, Crawford JD (2011) Intrinsic
881 reference frames of superior colliculus visuomotor receptive fields during head-
882 unrestrained gaze shifts. *J Neurosci* 31(50):18313-18326.
- 883 D'Esposito M, Postle BR (1999) The dependence of span and delayed-response
884 performance on prefrontal cortex. *Neuropsychologia* 37(11):1303-1315.
- 885 Dessing JC, Byrne PA, Abadeh A, Crawford JD (2012) Hand-related rather than
886 goal-related source of gaze-dependent errors in memory-guided reaching. *J Vis*
887 12(11). pii: 17. doi: 10.1167/12.11.17.
- 888 Dias EC, Segraves MA (1999) Muscimol-induced inactivation of monkey frontal eye
889 field: effects on visually and memory-guided saccades. *J Neurophysiol* 81:2191-
890 2214.
- 891 Everling S, Munoz DP (2000) Neuronal correlates of preparatory set associated with
892 pre-saccades and anti-saccades in the primate frontal eye field. *J Neurosci*
893 20(1):387-400.
- 894 Faisal AA, Selen LP, Wolpert DM (2008) Noise in the nervous system. *Nat Rev*
895 *Neurosci* 9:292-303.

896 Freedman EG, Sparks DL (1997) Activity of cells in the deeper layers of the superior
897 colliculus of the rhesus monkey: evidence for gaze displacement command. *J*
898 *Neurophysiol* 77(5):2328-2348

899 Funahashi S, Bruce CJ, Goldman-Rakic PS (1989) Mnemonic coding of visual
900 space in the monkey's dorsolateral prefrontal cortex. *J Neurophysiol* 61(2):331-349.

901 Funahashi S, Chafee MV, Goldman-Rakic PS (1993) Prefrontal neuronal activity in
902 rhesus monkeys performing delayed anti-saccade task. *Nature* 365:753-756.

903 Fuster JM (2001) The prefrontal cortex - an update: time is of the essence. *Neuron*
904 30:319-333.

905 Gaymard B, Ploner CJ, Rivaud-Pechoux S, Pierrot-Deseilligny C (1999) The frontal
906 eye field is involved in spatial short-term memory but not in reflexive saccade
907 inhibition. *Exp Brain Res* 129:288-301.

908 Gnadt JW, Andersen RA (1988) Memory related motor planning activity in posterior
909 parietal cortex of macaque. *Exp Brain Res* 70:216-220.

910 Gnadt JW, Bracewell RM, Andersen RA (1991) Sensorimotor transformation during
911 eye movements to remembered visual targets. *Vision Res* 34:93-106.

912 Goldman-Rakic PS (1987) Circuitry of primate prefrontal cortex and regulation of
913 behavior by representational memory. In *Handbook of Physiology – The Nervous*
914 *System V*, F. Plum and V. Mountcastle, eds. (Bethesda, Maryland: American
915 *Physiological Society*), pp. 373–417.

- 916 Gottlieb J, Goldberg ME (1999) Activity of neurons in the lateral intraparietal area of
917 the monkey during an antisaccade task. *Nat Neurosci* 2:906-912
- 918 Hawkins KM, Sayegh P, Yan X, Crawford JD, Sergio LE (2013) Neural activity in
919 superior parietal cortex during rule-based visual-motor transformations. *J Cogn*
920 *Neurosci* 25(3):436-454.
- 921 Heinzle J, Hepp K, Martin KAC (2007) A microcircuit model of the frontal eye fields.
922 *J Neurosci* 27:9341-9353.
- 923 Henriques DY, Klier EM, Smith MA, Lowy D, Crawford JD (1998) Gaze-centered
924 remapping of remembered visual space in an open-loop pointing task. *J Neurosci*
925 18(4):1583-1594
- 926 Johnston K, DeSouza JF, Everling S (2009) Monkey prefrontal cortical pyramidal
927 and putative interneurons exhibit differential patterns of activity between prosaccade
928 and antisaccade tasks. *J Neurosci* 29(17):5516-5524.
- 929 Keith GP, DeSouza JF, Yan X, Wang H, Crawford JD (2009) A method for mapping
930 response fields and determining intrinsic reference frames of single-unit activity:
931 Applied to 3D head-unrestrained gaze shifts. *J Neurosci Methods* 180:171-184.
- 932 Ketcham CJ, Hodgson TL, Kennard C, Stelmach GE (2003) Memory-motor
933 transformations are impaired in Parkinson's disease. *Exp Brain Res* 149:30-39.
- 934 Knight TA (2012) Contribution of the frontal eye field to gaze shifts in the head-
935 unrestrained rhesus monkey: neuronal activity. *Neuroscience* 225:213-236.

936 Krappmann P (1998) Accuracy of visually and memory-guided antisaccades in man.

937 Vision Res 38:2979-2985.

938 Kunzle H, Akert K, Wurtz RH (1976) Projection of area 8 (frontal eye field) to

939 superior colliculus in the monkey. An autoradiographic study. Brain Res 117(3):487-

940 492.

941 Lawrence BM, White RL, Snyder LH (2005) Delay-period activity in visual,

942 visuomovement, and movement neurons in the frontal eye field. J

943 Neurophysiol 94:1498-1508.

944 Ma WJ, Husain M, Bays PM (2014) Changing concepts of working memory. Nat

945 Neurosci 17(3):347-356.

946 Markowitz DA, Curtis CE, Pesaran B (2015) Multiple component networks support

947 working memory in prefrontal cortex. Proc Natl Acad Sci U S A 112(35):11084-

948 11089.

949 Martinez-Trujillo JC, Klier EM, Wang H, Crawford JD (2003) Contribution of head

950 movement to gaze command coding in monkey frontal cortex and superior colliculus.

951 J Neurophysiol 90(4):2770-2776.

952 Mazhari S, Badcock JC, Waters FA, Dragović M, Badcock DR, Jablensky A (2010)

953 Impaired spatial working memory maintenance in schizophrenia involves both spatial

954 coordinates and spatial reference frames. Psychiatry Res 179(3):253-258.

- 955 Mazzoni P, Bracewell RM, Barash S, Andersen RA (1996) Motor intention activity in
956 the macaque's lateral intraparietal areas. I. Dissociation of motor plan from sensory
957 memory. *J Neurophysiol* 76:1439-1456.
- 958 Minshew NJ, Luna B, Sweeney JA (1999) Oculomotor evidence for neocortical
959 systems but not cerebellar dysfunction in autism. *Neurology* 52(5):917-922.
- 960 Monteon JA, Avillac M, Yan X, Wang H, Crawford JD (2012) Neural mechanisms for
961 predictive head movement strategies during sequential gaze shifts. *J Neurophysiol*
962 108(10):2689-707. doi: 10.1152/jn.00222.2012.
- 963 Monteon JA, Constantin AG, Wang H, Martinez-Trujillo J, Crawford JD (2010)
964 Electrical stimulation of the frontal eye fields in the head-free macaque evokes
965 kinematically normal 3D gaze shifts. *J Neurophysiol* 104(6):3462-75. doi:
966 10.1152/jn.01032.2009.
- 967 Monteon JA, Wang H, Martinez-Trujillo J, Crawford JD (2013) Frames of reference
968 for eye-head gaze shifts evoked during frontal eye field stimulation. *Eur J Neurosci*
969 37(11):1754-65. doi: 10.1111/ejn.12175.
- 970 Offen S, Gardner JL, Schluppeck D, Heeger DJ (2010) Differential roles for frontal
971 eye fields (FEFs) and intraparietal sulcus (IPS) in visual working memory and visual
972 attention. *J Vis* 10:1-14.
- 973 Okamoto H, Isomura Y, Takada M, Fukai T (2007) Temporal integration by
974 stochastic recurrent network dynamics with bimodal neurons. *J Neurophysiol*
975 97:3859-3867.

- 976 Opris I, Barborica A, Ferrera VP (2003) Comparison of performance on memory-
977 guided saccade and delayed spatial match-to-sample tasks in monkeys. *Vision*
978 *Research* 43:321-332.
- 979 O'Sullivan EP, Jenkins IH, Henderson L, Kennard C, Brooks DJ (1995) The
980 functional anatomy of remembered saccades - a PET study. *Neuroreport* 6:2141-
981 2144.
- 982 Oyachi H, Ohtsuka K (1995) Transcranial magnetic stimulation of the posterior
983 parietal cortex degrades accuracy of memory-guided saccades in humans. *Invest*
984 *Ophthalmol Vis Sci* 36(7):1441-1449.
- 985 Paré M, Crommelinck M, Guitton D (1994) Gaze shifts evoked by stimulation of the
986 superior colliculus in the head-free cat conform to the motor map but also depend on
987 stimulus strength and fixation activity. *Exp Brain Res* 101(1):123-139.
- 988 Ploner CJ, Rivaud-Péchox S, Gaymard BM, Agid Y, Pierrot-Deseilligny C (1999)
989 Errors of memory-guided saccades in humans with lesions of the frontal eye field
990 and the dorsolateral prefrontal cortex. *J Neurophysiol* 82(2):1086-1090.
- 991 Postle BR (2006) Working memory as an emergent property of the mind brain.
992 *Neuroscience* 139:23-38.
- 993 Pouget A, Snyder LH (2000) Computational approaches to sensorimotor
994 transformations. *Nat Neurosci* 3:1192-1198.
- 995 Rainer G, Rao SC, Miller EK (1999) Prospective coding for objects in primate
996 prefrontal cortex. *J Neurosci* 19:5493-5505.

- 997 Rottschy C, Kleiman A, Dogan I, Langer R, Mirzazade S, Kronenbuerger M, Werner
998 C, Shah NJ, Schulz JB, Eickhoff SB, Reetz K (2013). Diminished activation of motor
999 working-memory networks in parkinson's disease. PLoS One 8(4):e61786. doi:
1000 10.1371/journal.pone.0061786.
- 1001 Sadeh M, Sajad A, Wang H, Yan X, Crawford JD (2015) Spatial transformations
1002 between superior colliculus visual and motor response field during head-
1003 unrestrained gaze shifts. Eur J Neurosci. Doi: 10.1111/ejn.13093.
- 1004 Sajad A, Sadeh M, Keith GP, Yan X, Wang H, Crawford JD (2015) Visual–motor
1005 transformations within frontal eye fields during head-unrestrained gaze shifts in the
1006 monkey. Cereb Cortex 25:3932-3952.
- 1007 Sato TR, Schall JD (2003) Effects of stimulus-response compatibility on neural
1008 selection in frontal eye field. Neuron 38:637-648.
- 1009 Segraves MA (1992) Activity of monkey frontal eye field neurons projecting to
1010 oculomotor regions of the pons. J Neurophysiol 68(6):1967-1985.
- 1011 Schall JD (2015) Visuomotor functions in the frontal lobe. Annu Rev Vis Sci 1:469-
1012 498.
- 1013 Simon SR, Meunier M, Piettre L, Berardi AM, Segebarth CM, Boussaoud D (2002)
1014 Spatial attention and memory versus motor preparation: premotor cortex
1015 involvement as revealed by fMRI. J Neurophysiol 88:2047-2057.

- 1016 Sommer MA, Wurtz RH (2001) Frontal eye field sends delay activity related to
1017 movement, memory, and vision to the superior colliculus. *J Neurophysiol* 85:1673-
1018 1685.
- 1019 Sparks DL, Porter JD (1983) Spatial localization of saccade targets. II. Activity of
1020 superior colliculus neurons preceding compensatory saccades. *J Neurophysiol*
1021 49:64-74.
- 1022 Stanford TR, Sparks DL (1994) Systematic errors for saccades to remembered
1023 targets: evidence for a dissociation between saccade metrics and activity in the
1024 superior colliculus. *Vision Res* 34:93-106.
- 1025 Sweeney JA, Mintun MA, Kwee S, Wiseman MB, Brown DL, Rosenberg DR, Carl JR
1026 (1996) Positron emission tomography study of voluntary saccadic eye movements
1027 and spatial working memory. *J Neurophysiol* 75(1):454-468.
- 1028 Sweeney JA, Luna B, Keedy SK, McDowell JE, Clementz BA (2007). fMRI studies of
1029 eye movement control: investigating the interaction of cognitive and sensorimotor
1030 brain systems. *Neuroimage* 36:T54-T60.
- 1031 Takaura K, Yoshida M, Isa T (2011) Neural substrate for spatial memory in the
1032 superior colliculus after damage to the primary visual cortex. *J Neurosci.* 31(11):
1033 4233-4241.
- 1034 Takeda K, Funahashi S (2002) Prefrontal task-related activity representing visual
1035 cue location or saccade direction in spatial working memory tasks. *J Neurophysiol*
1036 87:567-588.

- 1037 Takeda K, Funahashi S (2004) Population vector analysis of primate prefrontal
1038 activity during spatial working memory. *Cereb Cortex* 14:1328-1339.
- 1039 Takeda K, Funahashi S (2007) Relationship between prefrontal task-related activity
1040 and information flow during spatial working memory performance. *Cortex* 43(1):38-
1041 52.
- 1042 Verduzco-Flores S, Bodner M, Ermentrout B, Fuster JM, Zhou Y (2009) Working
1043 memory cells' behavior may be explained by cross-regional networks with synaptic
1044 facilitation. *PLoS One* 4(8):e6399. doi: 10.1371/journal.pone.0006399.
- 1045 Vesia M, Prime SL, Yan X, Sergio LE, Crawford JD (2010) Specificity of human
1046 parietal saccade and reach regions during transcranial magnetic stimulation. *J*
1047 *Neurosci* 30(39):13053-13065.
- 1048 Wang L, Li X, Hsiao SS, Lenz FA, Bodner M, Zhou YD, Fuster JM (2015).
1049 Differential roles of delay-period neural activity in the monkey dorsolateral prefrontal
1050 cortex in visual-haptic crossmodal working memory. *Proc Natl Acad Sci U S A*
1051 111(2):E214-219.
- 1052 Watanabe Y, Takeda K, Funahashi S (2009) Population vector analysis of primate
1053 mediodorsal thalamic activity during oculomotor delayed-response
1054 performance. *Cereb Cortex* 19:1313-1321.
- 1055 White JM, Sparks DL, Stanford TR (1994) Saccades to remembered target
1056 locations: an analysis of systematic and variable errors. *Vision Res* 34:79-92.

- 1057 Wimmer K, Nykamp DQ, Constantinidis C, Compte A (2014) Bump attractor
1058 dynamics in prefrontal cortex explains behavioral precision in spatial working
1059 memory. *Nat Neurosci* 17:431-439.
- 1060 Wurtz RH, Sommer MA, Paré M, Ferraina S (2001) Signal transformations from
1061 cerebral cortex to superior colliculus for the generation of saccades. *Vision*
1062 *Res* 41:3399-3412.
- 1063 Zelinsky GJ, Bisley JW (2015) The what, where, and why of priority maps and their
1064 interactions with visual working memory. *Ann N Y Acad Sci* 1339:154-164.
- 1065 Zhang M, Barash S (2004) Persistent LIP activity in memory antisaccades: Working
1066 memory for a sensorimotor transformation. *J Neurophysiol* 91:1424-1441.
- 1067 Zheng T, Wilson CJ (2002) Corticostriatal combinatorics: The implications of
1068 corticostriatal axonal arborizations. *J Neurophysiol* 87:1007-1017.

1069 **Figure 1.** An overview of the experimental paradigm and a conceptual schematic of
1070 the possible coding schemes in the FEF. A) Activity was recorded from single
1071 neurons in the FEF while monkeys performed memory-guided gaze task with the
1072 head free to move. Monkeys initially fixated a visual stimulus (black dot labeled *F*)
1073 for 400-500ms. A visual stimulus (black dot labeled *T*) was then briefly flashed on
1074 the screen for 80-100ms (left panel). After an instructed delay (variable in duration;
1075 450-850ms or 700-1500ms) the animal made a gaze shift to the remembered
1076 location of the target (gray dot labeled *T*) upon the presentation of the Go-signal.
1077 The Go-signal was the disappearance of the initial fixation target (gray dot labeled
1078 *F*). Inaccuracies in behavior were tolerated such that if final gaze landed within a
1079 window around the target a juice reward was provided. B) Five gaze trajectories to a
1080 single target (black circle) within a wide array of target (5×7 for this example
1081 session; gray dots) within the neuron's approximate RF location are shown. Initial
1082 fixation positions (tail of the trajectory) were randomly varied within a central zone
1083 (large gray circle) on a trial-by-trial basis. Final gaze positions (white circles) fell at
1084 variable positions around the target. Variability in initial and final positions (relative to
1085 different frames of reference) of target, gaze (i.e., eye in space), eye (in head), and
1086 head was used to spatially differentiate sensory and various motor parameters in
1087 various frames of reference. We exploited the variability in behavioral errors to
1088 differentiate between spatial models based on target position (*T*) and final gaze
1089 position (*G*). C) Additionally, a continuum of intermediary spatial models spanning *T*
1090 and *G* were constructed to treat spatial code as a continuous variable; this allowed
1091 us to trace changes in spatial code as activity evolved from vision to memory delay,

1092 during memory delay, and from memory delay to motor. D) shows some plausible
1093 schemes for the spatiotemporal evolution of neuronal code based on proposed
1094 theories: 1) The target code could be transformed into a gaze code early-on, and
1095 this gaze code maintained during memory (motor theory; light gray line), 2) the
1096 target code could be maintained in the memory (sensory theory; black line) and
1097 subsequently transformed into a gaze code upon movement initiation, or 3) the
1098 spatial code could gradually change from a target code to a gaze code (dark gray
1099 line).

1100 **Figure 2.** Approximate location of the FEF, the recorded sites in the two monkeys
1101 and population results corresponding to each. A) shows the anatomical location of
1102 the FEF, located at the anterior bank of the arcuate sulcus. B) Sites within the FEF
1103 from which neurons were recorded in each animal are plotted (circles) in the
1104 coordinates of the recording chamber with the center (0,0) approximately located at
1105 the stereotaxic coordinates corresponding to the FEF (see Materials and Methods).
1106 The black semi-circle represents the edge of the recording chamber. The color code
1107 represents the neuron type recorded from each site. Low-threshold microstimulation
1108 at these sites evoked saccades ranging from 2 degrees (at the most lateral sites)
1109 and 25 degrees (at the most medial sites) in head-restrained conditions (Bruce and
1110 Goldberg, 1985).

1111 **Figure 3.** An overview of the analysis methods for identifying spatial code and
1112 sampling neuronal activity from time-normalized activity profile. **A**, shows an
1113 example analysis for identifying the spatial code. Here, activity from early visual
1114 response (80-180ms after target onset) was sampled for analysis (**A-1**). **A-2**, shows
1115 the *T-G* continuum and three example RF-plots are shown for the visual response
1116 corresponding to the demarked models (arrows) along the *T-G* continuum. *T* is the
1117 eye-centered target model and *G* is the eye-centered gaze model. In the RF plots
1118 each circle represents firing rate data (diameter) for a single trial, plotted over
1119 position data corresponding to the tested model (in this study models spanning
1120 target model, *T*, and gaze model, *G*). The PRESS residuals are shown at the bottom
1121 of each RF plot. In each RF plot, the color code (blue-red scale corresponding to
1122 low-to-high) represents the non-parametric fit made to all data points. **A-3**, shows
1123 mean PRESS (y-axis) as a function of tested spatial model along the *T-G* continuum
1124 (x-axis). For this example visual response the best-fit model or spatial code (lowest
1125 PRESS residuals) is the intermediate model one step away from *T* (towards *G*).
1126 Although **A** shows analysis only for a single sampling window, for the main analyses
1127 reported in this study we sampled activity at 16 time-steps from visual response
1128 onset until gaze movement onset. For this we normalized the time between visual
1129 response onset until movement onset so we could collapse all trials together for
1130 analysis. **B**, shows the raster and spike density plots corresponding to the classic
1131 visually- (**B-1**) and movement- (**B-2**) aligned neuronal responses as well as the time-
1132 normalized spike density (**B-3**), and illustrates activity sampling based on each of
1133 these scheme

1134 **Figure 4.** A representative neuron with visual, delay, and movement responses, and
1135 results for the overall population. **A**, shows the visual- (left) and movement- (right)
1136 aligned raster and spike density plots for a VM neuron with sustained delay activity. The
1137 visual response of this neuron is from 65-300ms after target onset and the movement
1138 response begins 30ms before gaze onset. **B**, shows the time-normalized activity profile
1139 corresponding to **A** with the period between visual response (VR) onset and gaze
1140 movement onset normalized for all trials. **C**, show the RF maps for four time-steps (**C1** -
1141 **C4**) sampled from the time-normalized activity profile (**B**, light red shades) with the blue-
1142 to-red color gradient representing low-to-high neuronal activity levels. The best-fit model
1143 (i.e., spatial code) at each of these time-steps is depicted by a red triangle placed on the
1144 *T-G* continuum (panels above the RF plots). For this neuron there was a progressive
1145 but partial shift (three steps out of 10) in spatial code towards *G*. **D**, depicts the time-
1146 normalized spike density for the entire population ($n = 74$) including neurons with either
1147 visual or movement response or both. Neurons with movement-related activity
1148 beginning at or after gaze onset are eliminated. **E**, shows the mean (\pm SEM) of spatially-
1149 tuned best-fits at 16 half-overlapping time-steps from an early visual period (visual
1150 response onset for visually-responsive neurons, and 80ms after target onset if neuron
1151 was not visually responsive) until gaze movement onset time. The solid line shows the
1152 mean of the fits made to individual neuron data highlighting the change in the population
1153 spatial code along *T-G* continuum as activity progresses from vision to movement. The
1154 histogram in the bottom panel shows the percentage of neurons that exhibited spatial
1155 tuning (y-axis) at a given time-step (x-axis).

1156 **Figure 5.** Single neuron example and population results for visual (V) neurons. **A**,
1157 shows the time-normalized spike density profile for an example V neuron (top panel)
1158 and the data points corresponding to the spatially-tuned time-steps across 16 half-
1159 overlapping time-steps (bottom panel). The RF plot corresponding to the highlighted
1160 time-step (first time-step in pink) is shown with the spatial code highlighted above the
1161 plot. **B**, shows the population time-normalized post-stimulus time histogram (mean
1162 \pm SEM) and the mean (\pm SEM) of the spatially-tuned data points at these time-steps
1163 across the V population. Colored data points (bottom panel) correspond to time-steps at
1164 which the population spatial coherence was significantly higher than the pre-target
1165 baseline and gray shades correspond to eliminated time-steps with spatial coherence
1166 indistinguishable from pre-target baseline. The histogram shows the percentage of
1167 neurons at each time-step that exhibited spatial tuning. The baseline firing rate is
1168 calculated based on average firing rate in 100ms pre-target period is shown by the solid
1169 horizontal lines in spike density plots (**A** and **B** top panels). For reference, the
1170 approximate Visual, Delay, and Motor epochs are depicted at top of the panels.
1171

1172 **Figure 6.** Single neuron example and population results for visuomovement (VM)
1173 neurons. **A** and **B**, same conventions as Figure 5. **C**, The RF plots corresponding to
1174 time-steps with highlighted data points (green border circles) in **A** (bottom panel) are
1175 shown, with the spatial code along *T-G* continuum highlighted above each plot.

1176 **Figure 7.** Distribution of best-fit models across the *T-G* continuum for VM population
1177 through 5 time-steps through visual, delay and movement responses. **A**, shows the
1178 distribution of best-fits for VM neurons for early-visual (1st time-step from the time-
1179 normalized activity profile), early-delay (4th time-step), mid-delay (9th time-step), late-
1180 delay (13th time-step), and peri-movement (15th time-step) intervals. Only neurons with
1181 significant spatial tuning are considered. The number of neurons contributing to each
1182 distribution is indicated on each panel (the number in the brackets also includes best-fits
1183 outside of the presented range). **B**, plots the best-fit model describing the activity during
1184 each of the delay intervals (y-axis), versus the best-fit model describing the
1185 perimovement activity (red dots). Here, only the 21 neurons that contributed to all five
1186 panels in **A** were plotted. Note the trend (from the early to mid to late delay periods) for
1187 the data points to migrate towards the line of unity, i.e. toward their movement fits.

1188

1189 **Figure 8.** Spatiotemporal progression of neuronal code in VM neurons with sustained
1190 delay activity. **A**, shows the results with time-normalized activity sampling including
1191 visual and movement response using the same conventions as Figure 5B (bottom
1192 panel). **B**, shows the results for only the delay period, with visual and movement
1193 responses excluded. Specifically, activity was sampled from 12 half-overlapping steps
1194 from the end of visual response (on average 266ms after target onset) until the
1195 beginning of the movement response (on average 85ms before gaze onset). This
1196 duration was on average 635ms. **C**, shows spatial code at fixed-times intervals relative
1197 to specific task events: target onset (left), the Go-signal (middle) and gaze onset (right).
1198 For target-aligned analysis (**C**, left panel), time from 80ms after target onset and the
1199 earliest Go-signal was divided into 8 half-overlapping steps, resulting in sampling
1200 window size fixed for any session but ranging between 80 and 150ms depending on
1201 whether the earliest Go-signal appeared 450ms or 750ms relative to target onset for
1202 that session. The Go-signal-aligned analysis (**C**, middle panel) was performed using
1203 100ms half-overlapping windows starting 150ms before to 150ms after the Go-signal.
1204 The movement-aligned analysis (**C**, right panel) was performed using half-overlapping
1205 100ms sampling windows starting from 150ms before to 150ms after gaze onset.
1206 Notice that although there is no change in spatial code triggered by specific task events,
1207 there is a progressive change in spatial code from *T* towards *G* as we move away from
1208 time of target presentation (left panel) to the time of gaze onset (right panel) in
1209 agreement with the trend seen in **A** and **B**.

1210 **Figure 9.** Single neuron example and population results for delay-movement (DM)
1211 neurons. **A** and **B**, follow the same conventions as Figure 5. **C**, follows the same
1212 convention as Figure 6C. Since these neurons lacked a visual response neuronal
1213 activity sampling started from 80ms after target onset.

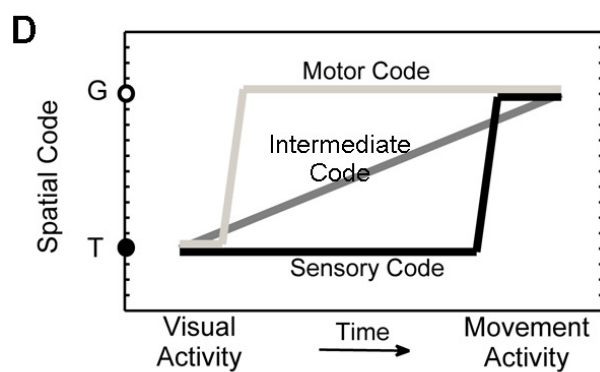
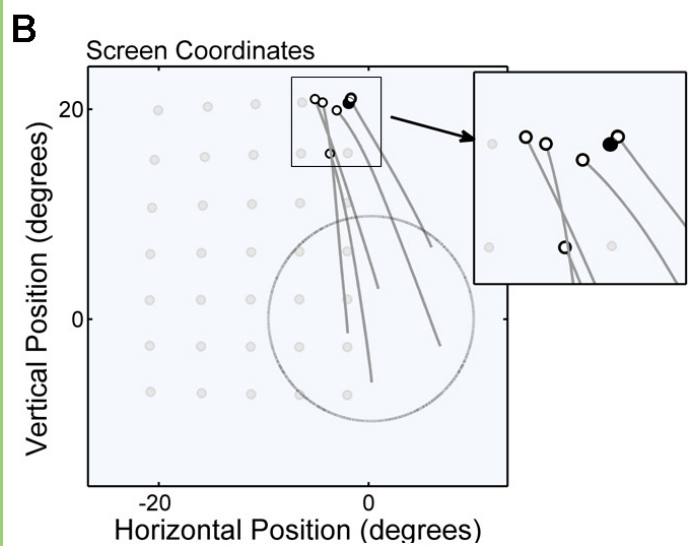
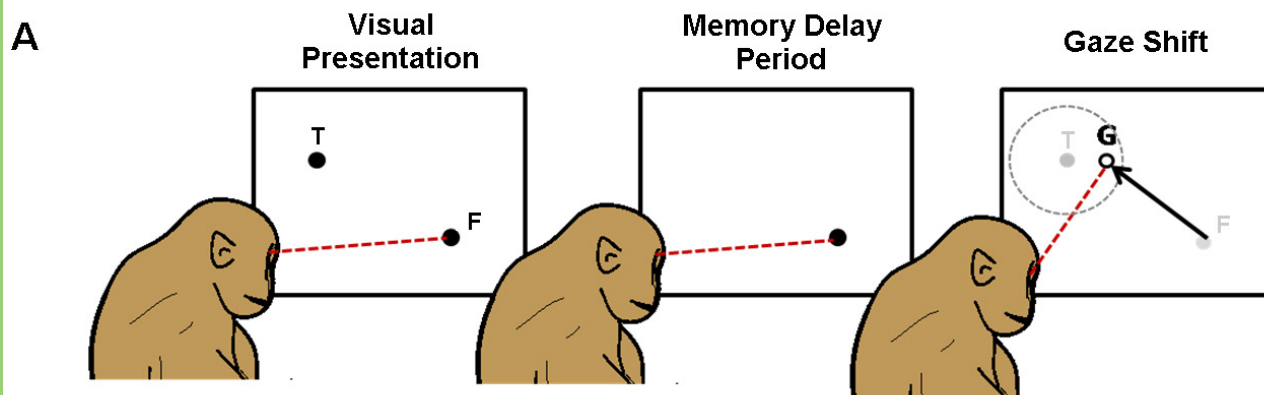
1214 **Figure 10.** Single neuron example and population results for movement-only (M)
1215 neurons. Same conventions as Figure 5 are used. Since these neurons lacked a visual
1216 response neuronal activity sampling started from 80ms after target onset.

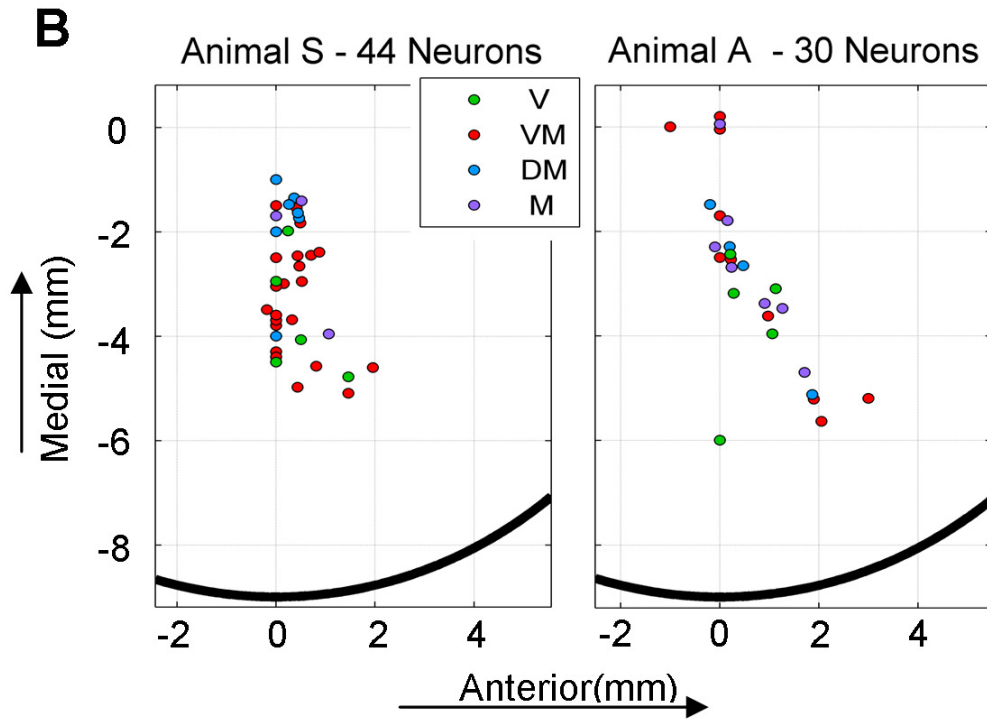
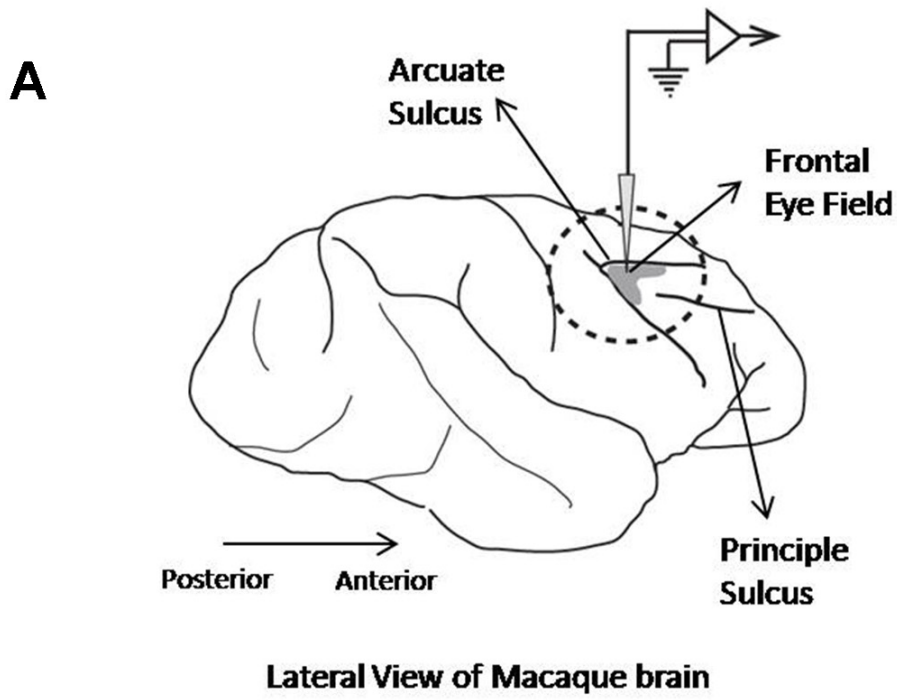
1217 **Figure 11.** Summary of the data for different neuron types and a proposed model of the
1218 flow of spatial information within the FEF. **A**, shows the relationship between the
1219 spatiotemporal codes of V (green), VM (red), DM (blue) and M (magenta) neurons.
1220 Asterisks (*) denote significant differences between neuron subtypes. **B**, shows a
1221 schematic of the possible flow of information. Target location information enters the FEF
1222 (but may already have undergone some spatial processing in VM neurons). The spatial
1223 code is maintained in working memory (WM), but monotonically changes towards *G* due
1224 to memory-related (mem) processes. Upon the presentation of the Go-signal, the most
1225 recent memory of target location (i.e., movement goal) is relayed to the motor (mot)
1226 circuitry (comprised of M neurons) which in turn encodes the metrics of the eminent
1227 gaze shift (*G*).

Statistical Table:

	Analysis	Data structure	Statistical test	Power
a	Monotonicity test for spatiotemporal code - entire population	y = spatial code, x = time-step	Spearman's ρ correlation	$R_s = 0.90, p = 2.44 \times 10^{-6}$
b	V population (1st time-step) code vs. T-code	Normality in V code distribution not assumed, n = 10	One-sample Wilcoxon Signed Rank Test	$p > 0.05$
c	VM population (1st time-step) code vs. T-code	Normality in V code distribution not assumed, n = 41	One-sample Wilcoxon Signed Rank Test	$p = 3.2 \times 10^{-5}$
d	Monotonicity test for spatiotemporal code - VM population	y = spatial code, x = time-step	Spearman's ρ correlation	$R_s = 0.91, p = 9.08 \times 10^{-7}$
e	VM population (final time-step) code vs. G-code	Normality in V code distribution not assumed, n = 40	One-sample Wilcoxon Signed Rank Test	$p = 3.51 \times 10^{-7}$
f	Early-delay (time-step 4) code vs. visual response (time-step 1) code	Normality in VM code distribution not assumed, n = 21	Paired-Sample Wilcoxon Signed Rank Test	$p = 0.302$
g	Late-delay (time-step 13) code vs. visual response (time-step 1) code	Normality in VM code distribution not assumed, n = 21	Paired-Sample Wilcoxon Signed Rank Test	$p = 0.0190$
h	Figure 7B: early-, mid-, and late-delay (time-steps 4, 9, 13) code vs. movement response (time-step 15) code	Normality in VM code distribution not assumed, n = 21	BonFerroni corrected; Wilcoxon test	$p < 0.05$ (see Fig 7B)
i	Monotonicity test for spatiotemporal code - VM neurons with sustained delay	y = spatial code, x = time-step	Spearman's ρ correlation	$R_s = 0.86, p = 2.40 \times 10^{-5}$
j	Monotonicity test for spatiotemporal code (during delay-only period) - VM neurons with sustained delay	y = spatial code, x = time-step	Spearman's ρ correlation	$R_s = 0.76, p = 0.0038$
k	DM population (final time-step) code vs. T-code	Normality in DM code distribution not assumed	One-sample Wilcoxon Signed Rank Test	$p = 4.88 \times 10^{-4}$
l	DM population (final time-step) code vs. G-code	Normality in DM code distribution not assumed	One-sample Wilcoxon Signed Rank Test	$p = 0.0015$
m	Monotonicity test for spatiotemporal code - DM population	y = spatial code, x = time-step	Spearman's ρ correlation	$R_s = 0.47, p = 0.20$
n	M population (final time-steps) code vs. G-code	Normality in M code distribution not assumed, n ≤ 10	One-sample Wilcoxon Signed Rank Test	$p > 0.20$

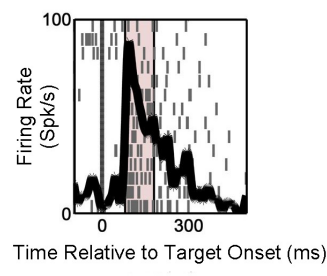
o	DM population vs. VM population code	Normality in neither population distribution is assumed	Mann-Whitney U test	$p > 0.25$ for each time-step
p	DM population vs. VM population spatiotemporal progression	Two slopes obtained from: $y = \text{spatial code}$, $x = \text{time-step}$	Linear regression comparison	$p = 0.87$
q1	VM population (motor epoch) vs. M population (motor epoch) code	Normality in neither population distribution is assumed	Bonferroni-corrected Mann-Whitney U test	$p = 6.16 \times 10^{-5}$
q2	DM population (motor epoch) vs. M population (motor epoch) code	Normality in neither population distribution is assumed	Bonferroni-corrected Mann-Whitney U test	$p = 3.49 \times 10^{-5}$
r	VM population (15th time-step) code vs. M neurons (15th time-step) but only neurons with preference for G-like codes	Normality in neither population distribution is assumed	Mann-Whitney U test	$p = 0.0127$



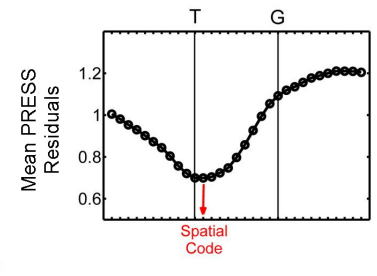


A) Spatial Analysis Method

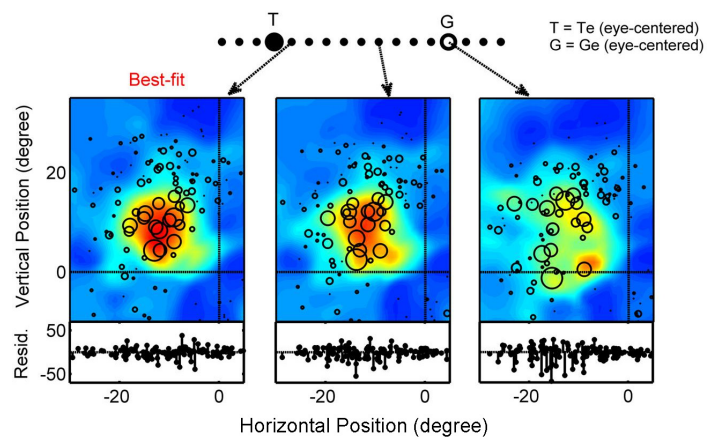
A-1) Sampled Activity



A-3) Identifying the Spatial Code

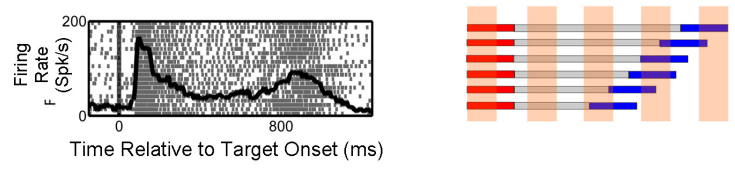


A-2) Tested Spatial Models: Target-Gaze Continuum

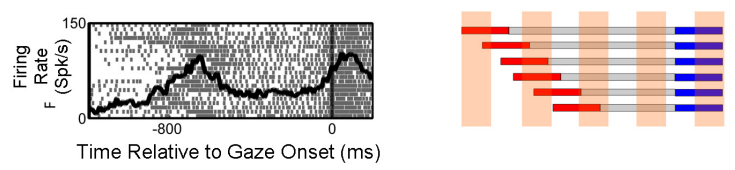


B) Time normalization and activity sampling

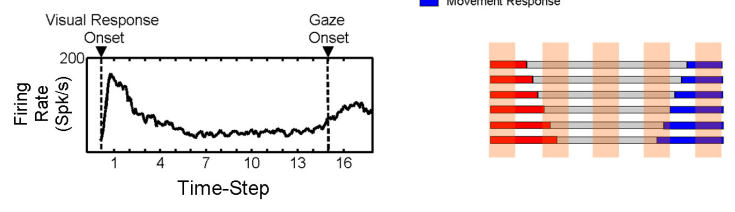
B-1) Visual Alignment of Neuronal Response

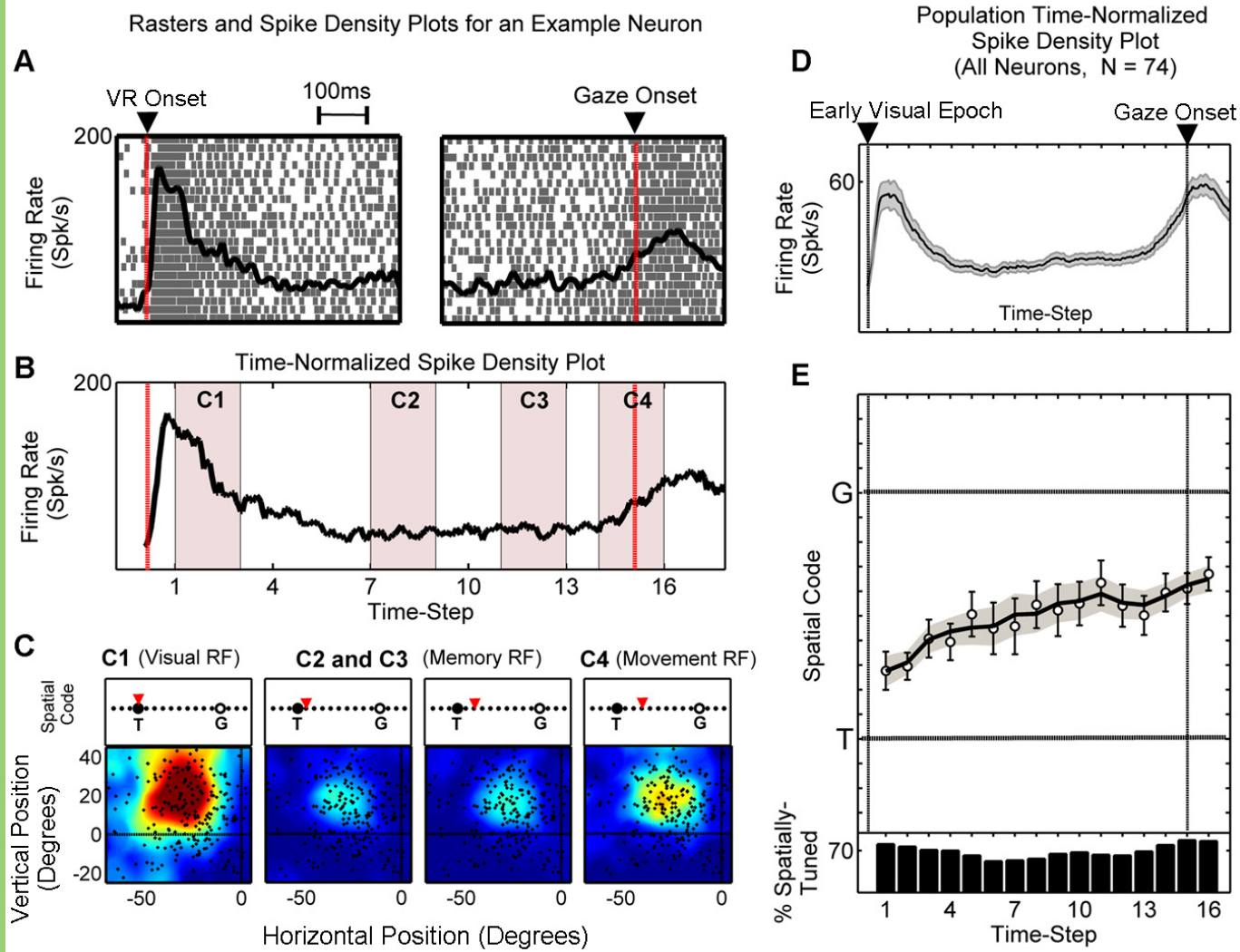


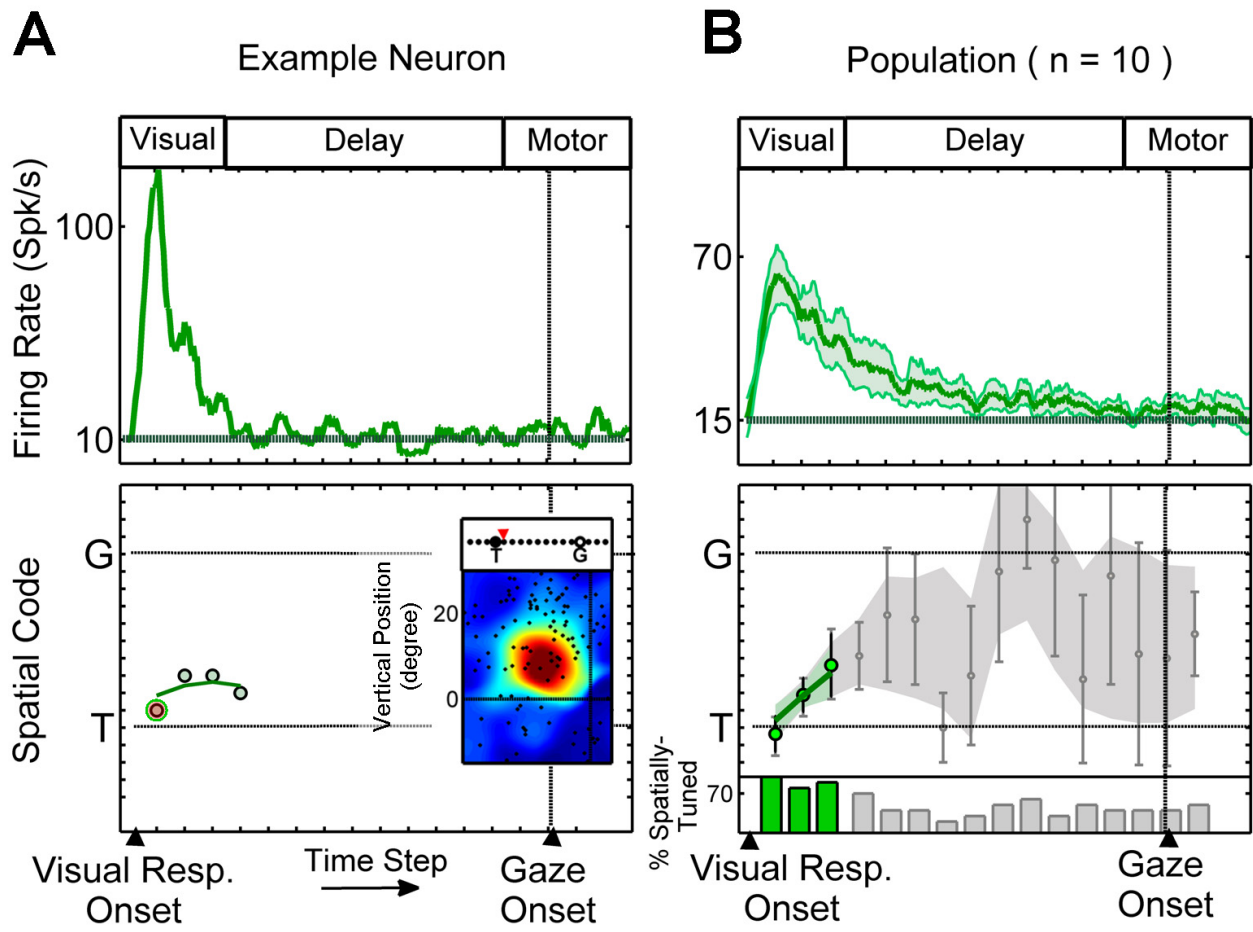
B-2) Movement Onset Alignment of Neuronal Response

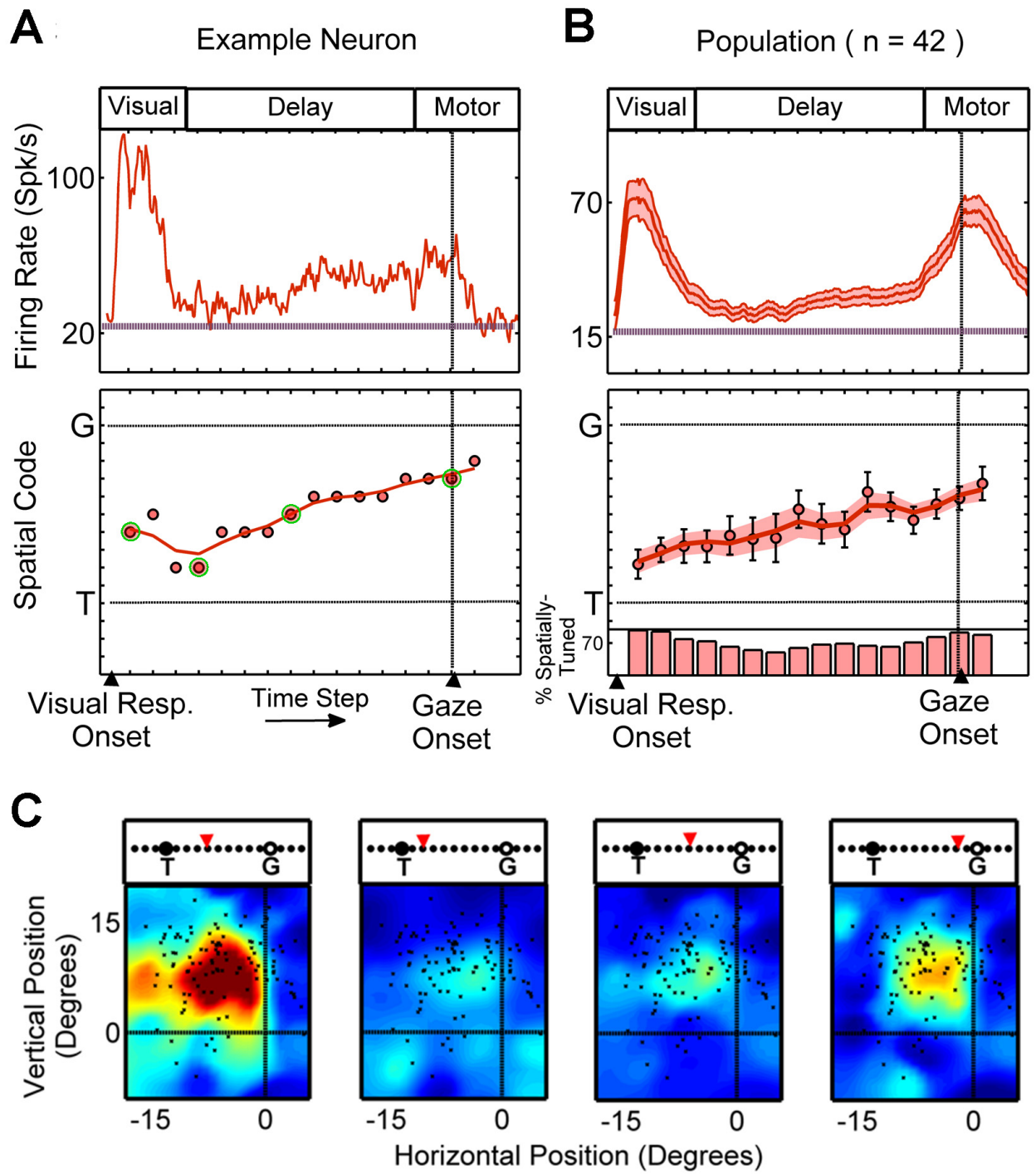


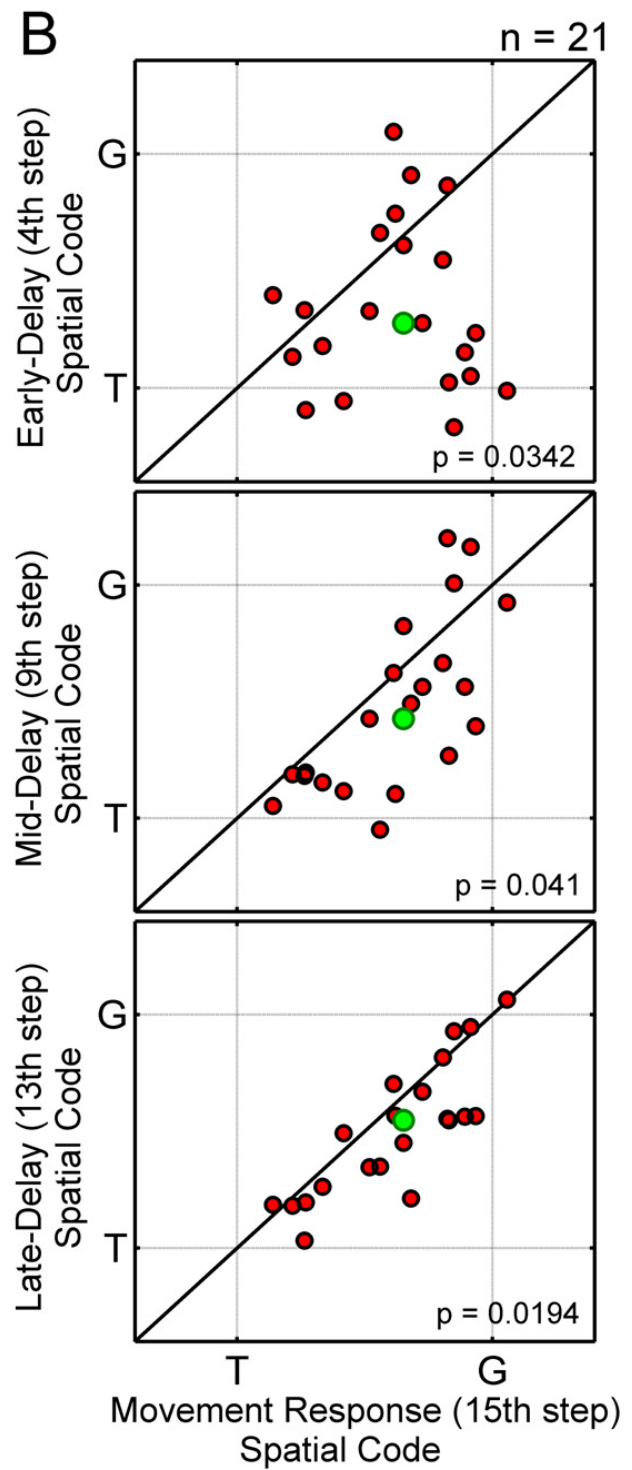
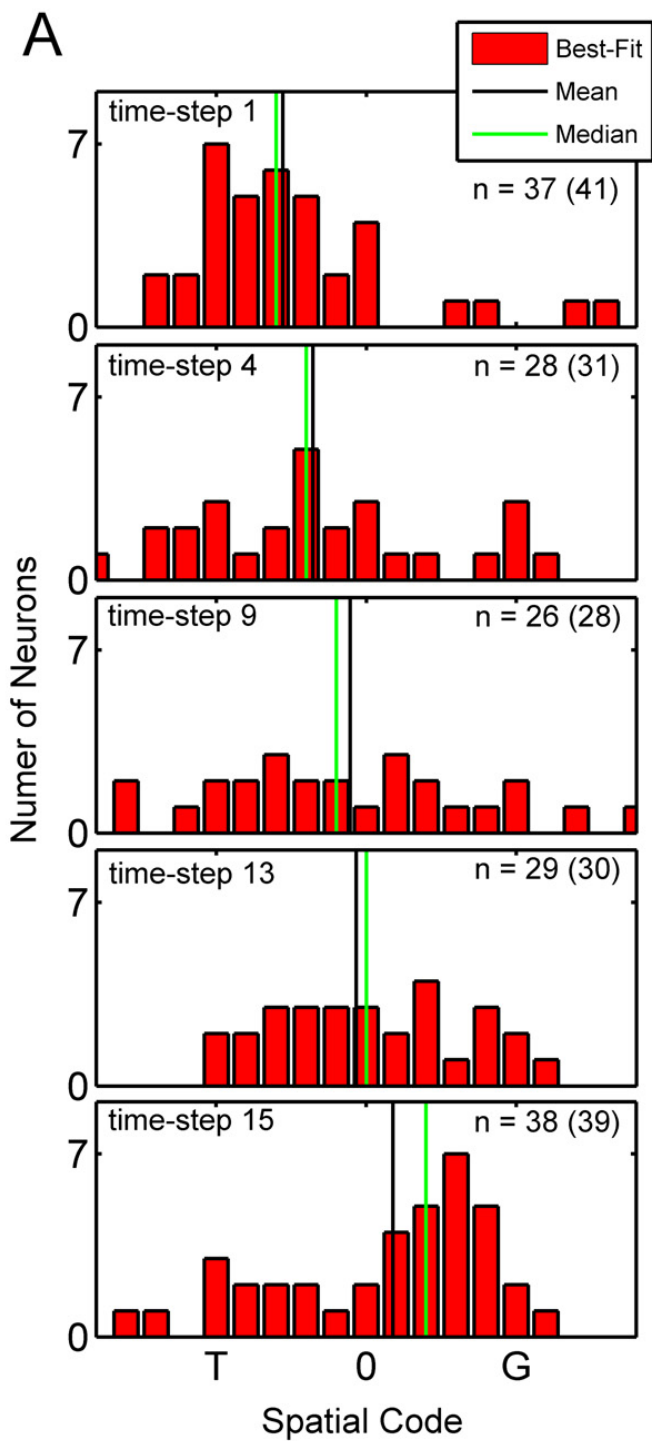
B-3) Time-Normalized Spike Density



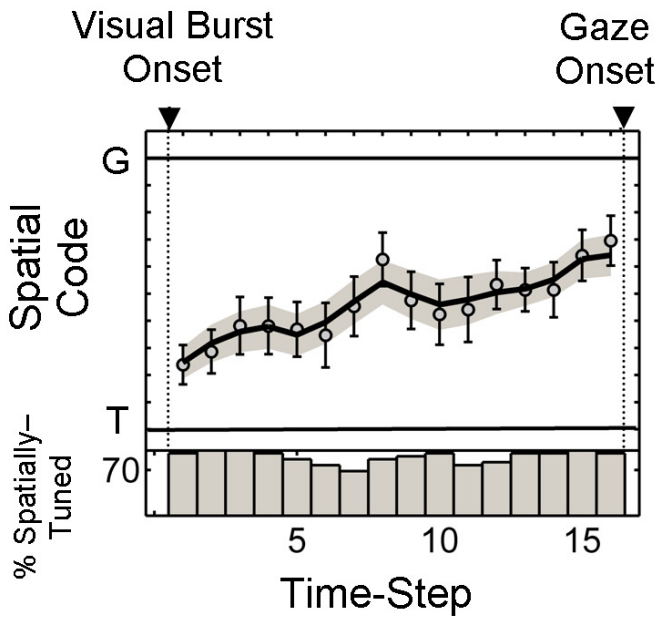




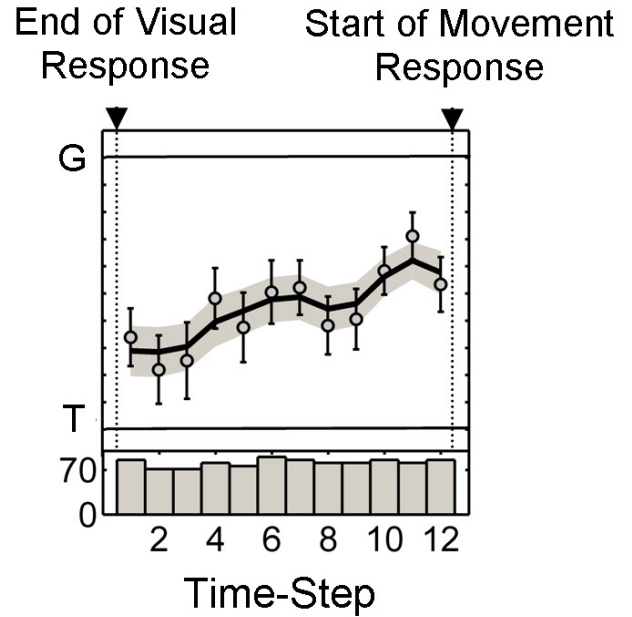




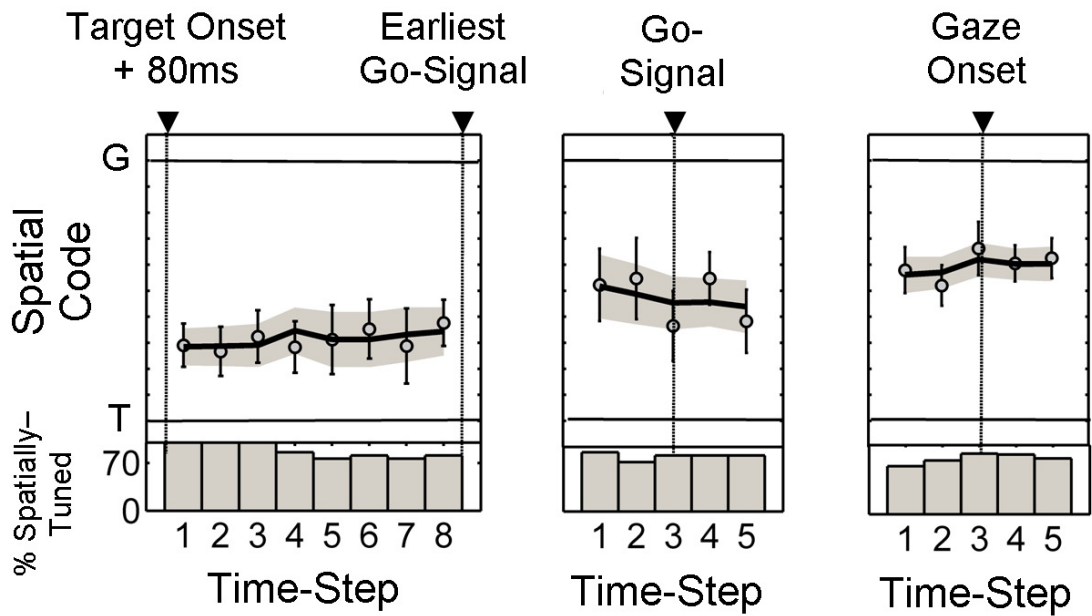
A) Entire Neuronal Response

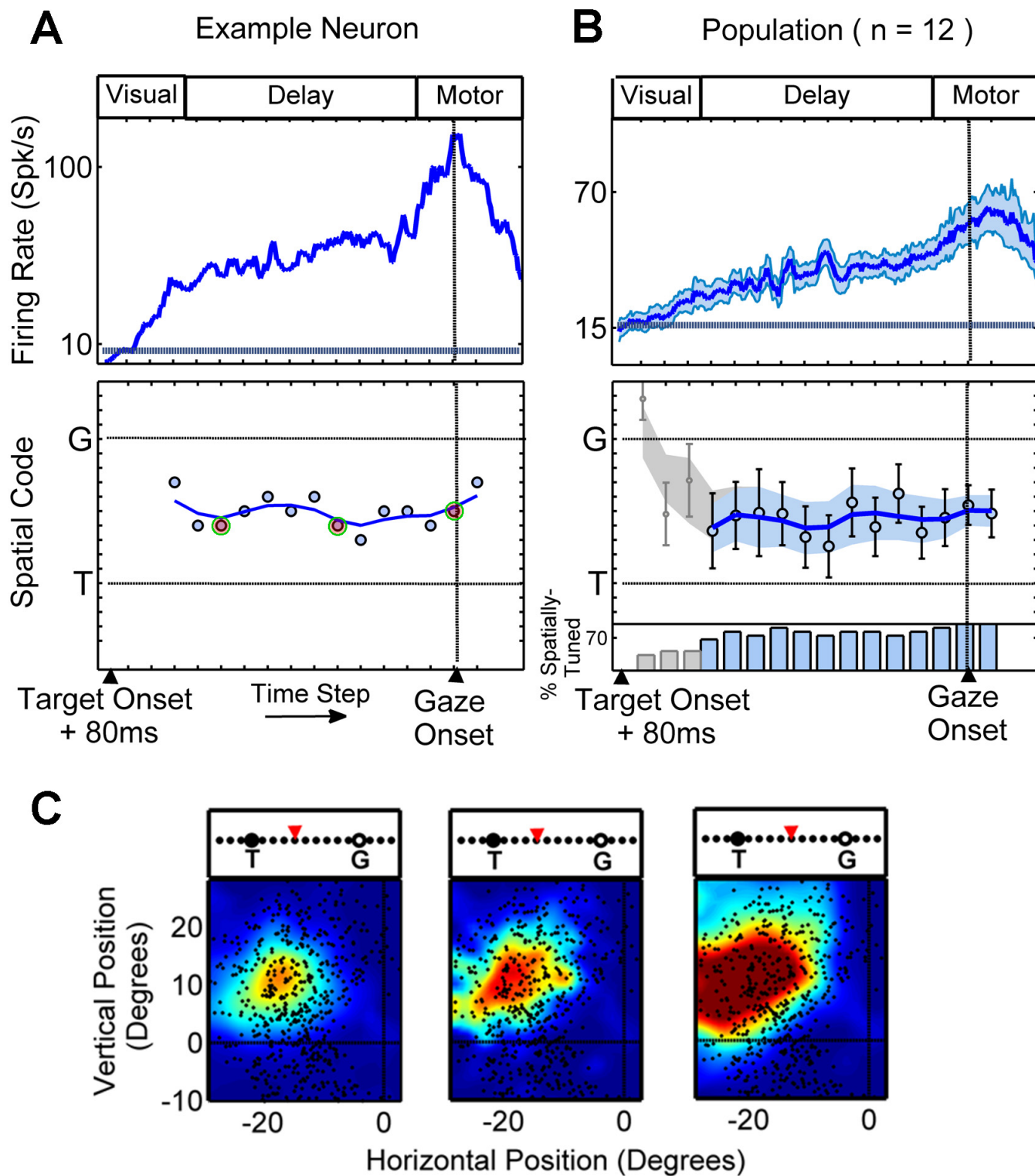


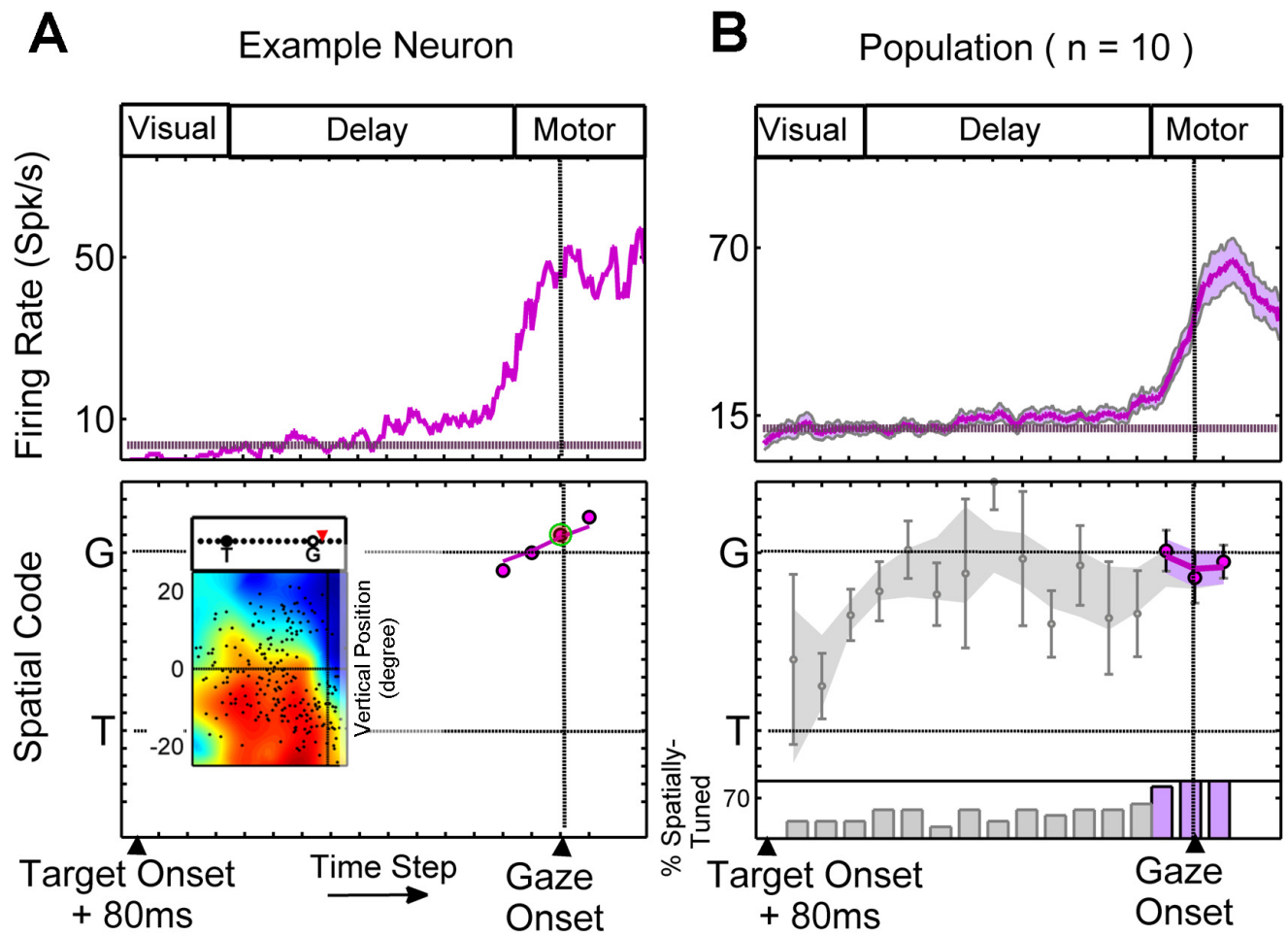
B) Delay Period Only



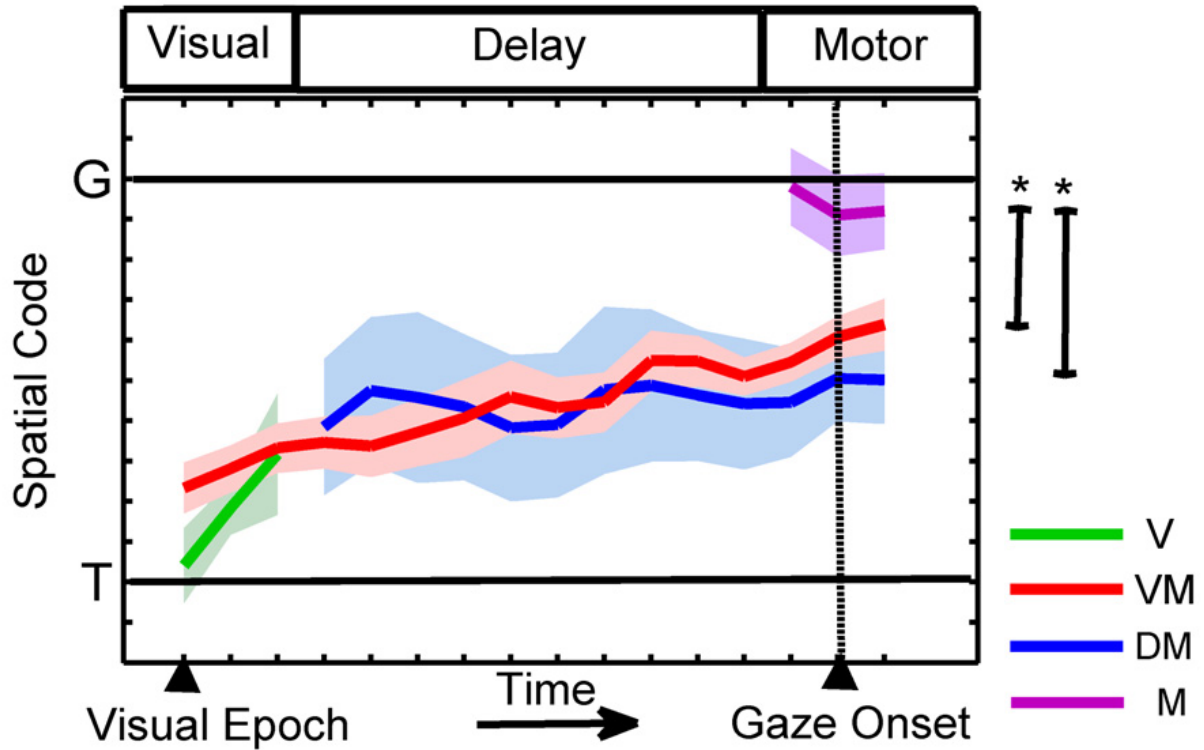
C) Relative to Specific Task Events







A) Spatial Codes in the FEF



B) Proposed Model

